# Portfolio Management with R

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## 1 Introduction

#### 1.1 About PMwR

This manual describes how to use the PMWR package. The aim of PMWR is to provide a small set of reliable, efficient and convenient tools that help in processing and analysing trade and portfolio data. The package does not provide a complete application that could be used 'as is'; rather, the package provides building blocks for creating such an application.

PMWR grew out of various pieces of software that I have written since 2008, first at the University of Geneva, later during my work at financial firms.

The package is currently under active development and changes frequently. This is mainly because the code has been written over many years and is in need of being groomed for general use. Consequently, this manual will change as frequently as the package.<sup>1</sup> I am grateful for comments and suggestions.

The latest version of the package is available from http://enricoschumann.net/R/packages/PMwR/index.htm. To install the package from within R, type

to download and install it. The package depends on several other packages, which are automatically obtained from the same repository and from CRAN. The source code is also pushed to a public repository at https://github.com/enricoschumann/PMwR.

There is currently no automatic build process for Windows. Recent versions of the package (since 0.3-4) are pure R code and can be built without any prerequisites except an R installation; older versions contained C code, so you needed to have the necessary tool chain installed (typically via Rtools). If you have problems building the package for Windows, please contact me and I will provide you with a Windows version.

 $<sup>^{1}</sup>$ The manual itself is written in Org mode. The complete tangled code is available from the website.

## 1.2 Principles

#### 1.2.1 Small

The aim of PMWR is to provide a *small* set of tools. This comes at the price: interfaces may be more complicated. But with few functions, it is easier to remember a function name or to find it in the first place.

#### 1.2.2 Flexible and general

PMWR aims to be open to different types of instruments, different timestamps, etc.

#### 1.2.3 Functional

With properly designed functions, it is possible to ignore how a job is done; knowing what is done is sufficient.

```
(K&R, chapter 1)
```

There are many good reasons for using functions.

- clearer code; easier to reuse; easier to maintain
- provide a clear view of what is needed for a specific computation; thus, they help with parallel/distributed computing
- · easier to test functionality
- input data is not changed
- · clean workspace after function call has ended

(There are more advantages, actually; such as the application of techniques such as memoisation.)

Computations provided by PMWR do not – for developers: should not – rely on global option-s/settings. The exception are functions that are used interactively, which essentially means print methods. (In scripts or methods, you should prefer cat.)

#### 1.2.4 Matching by name

Whenever possible and intuitive, data should be matched by name, not by position. This is most natural with vectors that store scalar information about instruments, such as prices or multipliers. In such cases, data input such as prices) is preferred in the form of named vectors.

#### 1.2.5 Vectorisation

Functions should do vectorisation when it is beneficial in terms of speed or clarity of code. Likewise, functions should work on matrices directly (typically columnwise) when it simplifies or speeds up things. Otherwise, applying the function (i.e. looping) should be left to the user.

An example may clarify this: drawdown is internally computed through cumsum, so it will be fast for a single vector. But for a matrix of time series, it would need a loop, which will be left to the user. On the other hand, returns can be computed very efficiently for a matrix.

## 1.3 Other packages

Several other packages originated from PMWR; initially, much of their code had been part of PMWR.

#### 1.3.1 datetimeutils

From the DESCRIPTION file:

Utilities for handling dates and times, such as selecting particular days of the week or month, formatting timestamps as required by RSS feeds, or converting timestamp representations of other software (such as 'MATLAB' and 'Excel') to R. The package is lightweight (no dependencies, pure R implementations) and relies only on R's standard classes to represent dates and times ('Date' and 'POSIXt'); it aims to provide efficient implementations, through vectorisation and the use of R's native numeric representations of timestamps where possible.

https://github.com/enricoschumann/datetimeutils

http://enricoschumann.net/R/packages/datetimeutils/

#### 1.3.2 textutils

From the DESCRIPTION file:

Utilities for handling character vectors that store human-readable text (either plain or with markup, such as HTML or Lagrange provides, in particular, functions that help with the preparation of plain-text reports (e.g. for expanding and aligning strings that form the lines of such reports); the package also provides generic functions for transforming R objects to HTML and to plain text.

https://github.com/enricoschumann/textutils

http://enricoschumann.net/R/packages/textutils

#### 1.3.3 tsdb

From the DESCRIPTION file:

A terribly-simple data base for time series. All series are saved as csv files. The package offers utilities for saving files in a standardised format, and for retrieving and joining data.

https://github.com/enricoschumann/textutils

http://enricoschumann.net/R/packages/textutils

## 1.4 Setting up R

In this manual, all R output will be presented in English. In case you run R in a different locale, but want to receive messages in English, type this:

```
Sys.setenv(LANGUAGE = "en")
```

## 2 Keeping track of transactions: journals

#### 2.1 Overview

The ultimate basis of many financial computations are lists of transactions. PMWR provides an S3 class journal for handling such lists. A journal is a list of atomic vectors, to which a class attribute is attached. (Thus, a journal is quite similar to a dataframe.) Such a list is created through the function journal. Methods should not rely on this list being sorted in any particular way: components of a journal should always be retrieved by name, never by position. (In this respect a journal differs from a dataframe, for which we can meaningfully refer to the *n*-th column.) A journal's components, such as amount or timestamp, are called *fields* in this manual.

The simplicity of the class is intended, because it is meant for interactive analyses. The user may – and is expected to – dissect the information in a journal at will; such dissections include removing the class attribute.

#### 2.2 Fields

What is actually stored in a journal is up to the user. A number of fields are, however, required for certain operations and so it is recommended that they be present:

**amount** The notional amount that is transacted. amount is, in a way, the most important property of a journal. When functions compute something from the journal (the number of transactions, say), they will often look at amount.

**timestamp** When did the transaction take place? A numeric or character vector; should be sortable.

price Well, price. (Well, there are many types of prices. The price specified in a journal may be used to compute profit/loss; therefore, the difference between prices should be proportional to profit/loss for the transactions. Unfortunately, there are many instruments that are not quoted in transaction prices: Options may be quoted in implied volatility, bonds in yield, etc.)

**instrument** Description of the financial instrument; typically an identifier, a.k.a. ticker or symbol. That is, a string or perhaps a number; but not a more-complex object (recall that journals are lists of atomic vectors).

id A transaction identifier, possibly but not necessarily unique.

**account** Description of the account.

```
... other fields. They must be named, as in fees = c(1,2,1)
```

All fields except amount can be missing. Such missing values will be 'added back' as NA with the exception of id and account, which will be NULL. To be clear: amount could be a vector of only NA values, but it cannot be left out when the journal is created. (This will become clearer with the examples below.)

A journal may have no transactions at all in it. In such a case all fields have length zero, e.g. amount would be numeric(0) and so on. Such empty journals may be created by saying journal() or by coercing a zero-row dataframe to a journal, via a call to as.journal.

Transactions in a journal may be organised in hierarchies, such as

```
account => subaccount => subsubaccont => ... => instrument
```

This is useful and necessary when you have traded an instrument for different accounts, say, or as part of different strategies. Such a hierarchy may be completely captured in the instrument field, by concatenating account hierarchy and instrument using a separator pattern such as ::.¹ The result would be 'namespaced' instruments such as Pension::Equities::AMZN. Alternatively, part of the hierarchy may be stored in the account field.

## 2.3 Creating and combining journals

The function journal creates journal objects. See ?journal for details about the function and about methods for journal objects. At its very minimum, a journal must contain amounts of something.

```
J \leftarrow journal(amount = c(1, 2, -2, 3))
J
```

Actually, that is not true. On occasion it is useful to create an empty journal, one with no entries at all. You can do so by saying journal(), without any arguments.

<sup>&</sup>lt;sup>1</sup>This notation is inspired by the syntax of ledger files. See http://www.ledger-cli.org/.

```
journal()
no transactions
```

To see the current balance, which is nothing more than the sum over all amounts, you can use position.

```
position(J)
4
```

Suppose you wanted to note how many bottles of milk and wine you have stored in your basement. Whenever you add to your stock, you have a positive amount; whenever you retrieve bottles, you have a negative amount. Then, by keeping track of transactions, you may not have to take stock (apart, perhaps, from occasional checking that you did not miss a transaction), as long as you keep track of what you put into your cellar and what you take out.

There may be some analyses you can do on flows alone: you may check your drinking habits for patterns, such as slow accumulation of wine, followed by rapid consumption; or the other way around. But typically, you will want to analyse your transactions later, and then the more information you record about them – when, what, why, at what price, etc. –, the better. Journals allow you to store such information. To show how they are used, let us switch to a financial example.

```
tmp <- orgutils::readOrg(text = "</pre>
      DATE | WHAT
                                        | FX | AMOUNT | COMMENT
| 2017-07-01 | Cash
                                       | EUR |
                                                4500 | initial balance |
| 2017-07-01 | Cash
                                                  0 | initial balance |
                                       | CHF |
| 2017-08-15 | Expenses::shopping
                                      | EUR |
                                                    45
2017-07-31 | Expenses::rent
                                      | EUR | 1300 |
| 2017-07-15 | Cash
                                      | EUR | -1200 |
| 2017-07-15 | Cash
                                      | CHF | 1400 |
2017-07-15 | Expenses::commission | EUR |
                                                  -10 I
| 2017-08-15 | Expenses::holidays:hotel | CHF |
                                                 900 |
| 2017-08-15 | Expenses::meals | CHF |
                                                  70
| 2017-08-15 | Expenses::shopping
| 2017-08-31 | Expenses::rent
                                                 170 |
                                       | CHF |
                                      | EUR | 1300 |
names(tmp) <- c("timestamp", "account",</pre>
               "instrument", "amount", "comment")
tmp$timestamp <- as.Date(tmp$timestamp)</pre>
J <- as.journal(tmp)</pre>
```

```
instrument
                timestamp
                          amount
                                                   account
                                                                   comment
          EUR 2017-07-01
                                                      Cash initial balance
1
                          4500
2
          CHF 2017-07-01
                              0
                                                      Cash initial balance
          EUR 2017-08-15
                              45
3
                                        Expenses::shopping
          EUR 2017-07-31
                           1300
                                           Expenses::rent
5
          EUR 2017-07-15
                          -1200
                                                      Cash
          CHF 2017-07-15
                          1400
6
                                                      Cash
                            -10
7
          EUR
               2017-07-15
                                      Expenses::commission
8
               2017-08-15
                             900 Expenses::holidays:hotel
          CHF
9
          CHF
               2017-08-15
                             70
                                           Expenses::meals
10
          CHF
               2017-08-15
                             170
                                        Expenses::shopping
11
          EUR 2017-08-31
                            1300
                                           Expenses::rent
11 transactions
```

A print method defines how a journal is displayed. See ?print.journal for details. In general, you can always get help for methods for generic functions by saying ?<generic\_function>.journal, e.g. ?print.journal or ?as.data.frame.journal.

A str method shows the fields in the journal.

```
str(J)
```

```
'journal': 11 transactions
$ instrument: chr [1:11] "EUR" "CHF" "EUR" "EUR" ...
$ account : chr [1:11] "Cash" "Cash" "Expenses::shopping" ...
$ timestamp : chr [1:11] "2017-07-01" "2017-07-01" "2017-08-15" ...
$ amount : int [1:11] 4500 0 45 1300 -1200 1400 -10 900 70 170 ...
$ price : logi [1:11] NA NA NA NA NA NA ...
$ comment : chr [1:11] "initial balance" "initial balance" "" ...
```

You may notice that the output is similar to that of a data.frame or list. That is because J is a list of atomic vectors, with a class attribute. Essentially, it is little more than a list of the columns of the above table. (But note in the output of str(J) that journal silently added a price field, even though we did not specify one.)

In the example, the timestamps are of class Date. But essentially, any vector of mode character or numeric can be used, for instance POSIXct, or other classes. Here is an example that uses the nanotime package (Eddelbuettel, 2017).

```
timestamp amount
1 1519764172896552001 1
2 1519764172896552002 2
3 1519764172896552003 3

3 transactions
```

#### Journals can be combined with c.

```
J2 <- J
J2$remark <- rep("new", length(J))
c(J, J2)</pre>
```

inc	trument	timestamp	amount	account		comment
remark	trument	timestamp	amount	account		Comment
1	EUR	2017-07-01	4500	Cash	initial	balance
<na></na>						
2	CHF	2017-07-01	0	Cash	initial	balance
<na></na>						
3	EUR	2017-08-15	45	Expenses::shopping		
<na></na>						
4	EUR	2017-07-31	1300	Expenses::rent		
<na></na>						
5	EUR	2017-07-15	-1200	Cash		
<na></na>	CHE	2017 07 15	1 4 0 0	0 !		
6	CHF	2017-07-15	1400	Cash		
<na> 7</na>	EUR	2017-07-15	-10	Expenses::commission		
/ <na></na>	LUK	2017-07-15	-10	expenses::Commission		
8	CHF	2017-08-15	900	Expenses::holidays:hotel		
<na></na>	CIII	2017 00 13	300	Expensesnorradys.noter		
9	CHF	2017-08-15	70	Expenses::meals		
<na></na>						
10	CHF	2017-08-15	170	Expenses::shopping		
<na></na>						
11	EUR	2017-08-31	1300	Expenses::rent		
<na></na>						
12	EUR	2017-07-01	4500	Cash	initial	balance
new						
13	CHF	2017-07-01	0	Cash	initial	balance
new						
14	EUR	2017-08-15	45	Expenses::shopping		
new						
15	EUR	2017-07-31	1300	Expenses::rent		
new						

#### 2 Keeping track of transactions: journals

16	EUR	2017-07-15	-1200	Cash		
new						
17	CHF	2017-07-15	1400	Cash		
new						
18	EUR	2017-07-15	-10	Expenses::commission		
new						
19	CHF	2017-08-15	900	Expenses::holidays:hotel		
new						
20	CHF	2017-08-15	70	Expenses::meals		
new						
21	CHF	2017-08-15	170	Expenses::shopping		
new						
22	EUR	2017-08-31	1300	Expenses::rent		
new						
22 transactions						

The new combined journal will not be sorted by date. (In general, a journal need not be sorted in any particular way.)

```
sort(c(J, J2))
```

```
instrument timestamp amount account
                                            comment remark
   EUR 2017-07-01 4500 Cash initial balance <NA>
1
                       0
2
        CHF 2017-07-01
                               Cash initial balance <NA>
        EUR 2017-07-01
                      4500
                               Cash initial balance
                                                     new
                       0
4
        CHF 2017-07-01
                               Cash initial balance
                                                     new
        EUR 2017-07-15 -1200
5
                               Cash
                                                     <NA>
[ ....]
22 transactions
```

We can also sort by some other field, for instance amount.

```
sort(c(J, J2), by = "amount", decreasing = TRUE)
```

```
instrument timestamp amount
                                                account
                                                                   comment remark
          EUR 2017-07-01 4500
1
                                                   Cash initial balance
                                                                               <NA>
            EUR 2017-07-01 4500
                                                   Cash initial balance
2
                                                                               new
           CHF 2017-07-15 1400 Cash
CHF 2017-07-15 1400 Cash
EUR 2017-07-31 1300 Expenses::rent
3
                                                                               <NA>
                                                                               new
5
                                                                               <NA>
[ ....]
22 transactions
```

## 2.4 Selecting transactions

In an interactive session, you can use subset to select transactions.

With subset, you need not quote the expression that selects trades and you can directly access a journal's fields. Because of the way subset evaluates its arguments, it should not be used within functions. (See the Examples section in ?journal for what can happen then.)

More generally, to extract or change a field, use its name, either through the \$ operator or double brackets  $[[\ldots]]^2$ 

```
J$amount

[1] 4500 0 45 1300 -1200 1400 -10 900 70

[10] 170 1300
```

You can also replace specific fields.

```
J$comment[1] <- "initial balance EUR"

instrument timestamp amount account comment

EUR 2017-07-01 4500 Cash initial balance EUR

CHF 2017-07-01 0 Cash initial balance

[....]</pre>
```

The `[` method works with integers or logicals, returning the respective transactions.

```
J[2:3]
```

<sup>&</sup>lt;sup>2</sup>The behaviour of '[[' may change in the future: it may then be used to iterate over the transactions in a journal, not the fields. This would be motivated by https://developer.r-project.org/blosxom.cgi/R-devel/NEWS/2016/03/09 even though the commit was reversed two days later https://developer.r-project.org/blosxom.cgi/R-devel/NEWS/2016/03/11

#### 2 Keeping track of transactions: journals

2 transactions

You can also pass a string, which is then interpreted as a regular expression that is matched against all character fields in the journal.

You can also specify the fields to match the string against.

```
J["Cash", match.against = "instrument"]
no transactions
```

By default, case is ignored, but you can set ignore.case to FALSE.

```
J["Cash"]

instrument timestamp amount account comment

EUR 2017-07-01 4500 Cash initial balance EUR

CHF 2017-07-01 0 Cash initial balance

EUR 2017-07-15 -1200 Cash

CHF 2017-07-15 1400 Cash

transactions
```

```
J["cash", ignore.case = FALSE]
no transactions
```

## 2.5 Computing balances

5935

EUR

#### 2.5.1 Computing positions from journals

The function position gives the current balance of all instruments.

```
position(J)

2017-08-31
CHF 2540
```

To get the position at a specific date, use the when argument.

```
position(J, when = as.Date("2017-07-10"))
```

```
2017-07-10
CHF 0
EUR 4500
```

If you do not like such a tabular view, consider splitting the journal.

```
lapply(split(J, J$instrument),
    position, when = as.Date("2017-07-10"))
```

```
$CHF
    2017-07-10
CHF    0
$EUR
    2017-07-10
EUR    4500
```

To get a time series of positions, you can use specific keywords for when: all will print the position at all timestamps in the journal.

```
position(J, when = "all")
```

```
CHF EUR

2017-07-01 0 4500

2017-08-15 2540 4635

2017-07-31 1400 4590

2017-07-15 1400 3290

2017-08-31 2540 5935
```

#### 2 Keeping track of transactions: journals

Keywords first and last give you the first and last position. (The latter is the default; so if when is not specified at all, the last position is computed.)

endofday computes the positions at the ends of calendar days in the journal; endofmonth prints the positions at the ends of all calendar months between the first and the last timestamp.

We are not limited to the timestamps that exist in the journal.

```
CHF EUR

2017-07-10 0 4500

2017-07-11 0 4500

2017-07-12 0 4500

2017-07-13 0 4500

2017-07-14 0 4500

2017-07-15 1400 3290

2017-07-16 1400 3290

2017-07-17 1400 3290

2017-07-18 1400 3290

2017-07-19 1400 3290

2017-07-20 1400 3290
```

By default, position will show you positions of all instruments, even if they are zero.

```
position(J, when = as.Date("2017-7-1"))

2017-07-01

CHF 0

EUR 4497
```

You can suppress such positions with drop.zero.

```
position(J, when = as.Date("2017-7-1"), drop.zero = TRUE)

2017-07-01

EUR 4497
```

drop. zero can also be a numeric value, in which case is it interpreted as an absolute tolerance. This is useful in cases such as this one:

```
2012-01-05
USD 2.775558e-17
```

(Note that there is no output.)

As a final example, when accounts are specified, we may also aggregate positions by account.

```
position(J, use.account = TRUE)
```

```
Cash
|-- CHF
                 1400
`-- EUR
                 3300
Expenses
   |-- commission
   | `-- EUR
                  -10
   |-- holidays
      `-- hotel
          '-- CHF 900
   |-- meals
   | `-- CHF
                  70
   |-- rent
   | '-- EUR 2600
   `-- shopping
       |-- CHF
                  170
       `-- EUR
                  45
```

## 2.6 Aggregating and transforming journals

Often the data provided by journals needs to be processed in some way. A straightforward strategy is to call as.data.frame on the journal and then to use one of the many functions and methods that can be used for dataframes, such as aggregate or apply.

Even without coercion to a dataframe: A journal is a list of atomic vectors and hence already very similar to a dataframe. As a consequence, many computations can also be done directly on the journal, in particular with tapply. An example: you have a journal trades and want to compute monthly turnover (two-way). If there is only one instrument or all instruments may be added without harm, you can use this expression:

```
tapply(trades,
        INDEX = format(jnl$timestamp, "%Y-%m"),
        FUN = function(x) sum(abs(x$amount)))
```

To break it down by instrument, just add instrument as a second grouping variable to the INDEX argument.

A special case is when a journal is to be processed into a new journal. For this, PMWR defines an aggregate method for journals. The method splits the journal according to the grouping argument by, which can be a list (as in the default method) or an atomic vector.

The argument FUN can either be a function or list. If a function, it should receive a journal and also evaluate to a journal. (Note that this is different from R's aggregate.data.frame, which calls FUN on all columns, but in turn cannot address specific columns of the data.frame.)

If FUN is a list, its elements should be named functions. The names should match fields in the journal.

An example: we have a journal covering two trading days and wish to create a summary journal, which aggregates buys and sells for every day.

```
J \leftarrow journal(timestamp = structure(c(15950, 15951, 15950, 15951, 15950,
                                  15950, 15951, 15951, 15951, 15951),
                                class = "Date"),
            amount = c(-3, -4, -3, -1, 3, -2, 1, 3, 5, 3),
            price = c(104, 102, 102, 110, 106, 104, 104, 106, 108, 107),
            fun <- function(x) {</pre>
   journal(timestamp = as.Date(x$timestamp[1]),
          amount = sum(x$amount),
          price = sum(x$amount*x$price)/sum(x$amount),
          instrument = x$instrument[1L])
}
aggregate(J,
         by = list(J$instrument,
                  sign(J$amount),
                  as.Date(J$timestamp)),
         FUN = fun)
```

### 2.6 Aggregating and transforming journals

```
instrument timestamp amount price

A 2013-09-02 -3 102.0000

B 2013-09-02 -5 104.0000

B 2013-09-02 3 106.0000

A 2013-09-03 -1 110.0000

B 2013-09-03 -4 102.0000

A 2013-09-03 9 107.2222

B 2013-09-03 3 106.0000

7 transactions
```

## 3 Computing profit and loss

In this chapter we will deal with computing profit and loss (P/L) measured in amounts of currency. If you are interested in computing returns, see Section Computing returns.

## 3.1 Simple cases

### 3.1.1 Total P/L

We buy one unit of an asset at a price of 100 euro and we sell it for 101. We have made a profit of 1 euro.

This simple case is frequent enough that we should make the required computation simple as well. The PMWR package provides a function pl, which for this case may be called as follows.

```
pl(price = c(100, 101),
  amount = c(1, -1)
```

```
P/L total
average buy 100
average sell 101
cum. volume
'P/L total' is in units of instrument;
'volume' is sum of /absolute/ amounts.
```

Instead of a vectors price and amount, you could also have passed a journal to pl.

In principle, P/L is straightforward to compute. Let x be a vector of the absolute amounts traded, and let p be a vector of the prices at which we traded. Then P/L is just the difference between what we received when selling and what we paid when buying.

$$\sum x_i^{\text{sell}} p_i^{\text{sell}} - \sum x_i^{\text{buy}} p_i^{\text{buy}}$$
(3.1)

This can be simplified when we impose the convention that sold amounts are negative.

$$P/L = -\sum_{x<0} x_i p_i - \sum_{x>0} x_i p_i$$

$$= -\sum_{x>0} x_i p_i$$
(3.2)

$$= -\sum x_i p_i \tag{3.3}$$

The function p1 also expects this convention: in the code example we had x = [1, -1]'.

There are several ways to perform this basic (or fundamental, rather) computation. Here are some, along with some timing results.

```
amount <- rep(c(-100,100), 100)
price <- rep(100, length(amount))

library("rbenchmark")
benchmark(
   amount %*% price,
   sum(amount*price),
   crossprod(amount, price),
   t(amount*price) %*% rep(1, length(amount)),
   columns = c("test", "elapsed", "relative"),
   order = "relative",
   replications = 20000)</pre>
```

pl uses the straightforward sum(amount \* price) variant; only when very long vectors are used, it switches to crossprod.

pl also accepts an argument instrument: if it is available, pl computes and reports P/L for each instrument separately. As an example, suppose you traded shares of two German companies, Adidas and Commerzbank. We collect the transactions in a journal.

```
J <- readOrg(text = "
| instrument | amount | price |
|-------|
| Adidas | 50 | 100 |
| Adidas | -50 | 102 |
| Commerzbank | 500 | 8 |
| Commerzbank | -500 | 7 |
")
J <- as.journal(J)
J</pre>
```

```
instrument amount price

1 Adidas 50 100

2 Adidas -50 102

3 Commerzbank 500 8

4 Commerzbank -500 7
```

We can now pass the journal directly to pl.

```
pl(J)
```

```
Adidas

P/L total 100
average buy 100
average sell 102
cum. volume 100

Commerzbank

P/L total -500
average buy 8
average sell 7
cum. volume 1000

'P/L total' is in units of instrument;
'volume' is sum of /absolute/ amounts.
```

An aside: since the shares are denominated in the same currency (euro), total profit is the same even if we had left out the instruments; however, average buying and selling prices becomes less informative.

Financial instruments differ not only in the currencies in which they are denominated. Many derivatives have multipliers, which you may also specify. Suppose you have traded FGBL (German Bund futures) and FESX (EURO STOXX 50 futures).

One point of the FGBL translates into 1000 euros; for the FESX it is 10 euros.

6 transactions

```
FESX JUN 16
 P/L total -250
 average buy 2910
 average sell 2905
 cum. volume 10
FGBL JUN 16
 P/L total 10
 average buy 164.12
 average sell 164.13
 cum. volume 2
FGBL MAR 16
 P/L total 170 average buy 165.2
 average sell 165.37
 cum. volume 2
'P/L total' is in units of instrument;
'volume' is sum of /absolute/ amounts.
```

Note that we used a named vector to pass the multipliers. Per default, the names of this vector need to exactly match the instruments' names. Setting multiplier.regexp to TRUE causes the names of the multiplier vector to be interpreted as (Perl-style) regular expressions.

At this point, it may be helpful to describe how we can access the results of such P/L computations (other than having them printed to the console, that is). The function pl always returns a list of lists – one list for each instrument.

```
str(futures_pl)
```

```
List of 3

$ FESX JUN 16:List of 6

..$ pl : num -250

..$ realised : logi NA

..$ unrealised: logi NA

..$ buy : num 2910

..$ sell : num 2905

..$ volume : num 10

$ FGBL JUN 16:List of 6

..$ pl : num 10

..$ realised : logi NA

..$ unrealised: logi NA
```

```
..$ buy
         : num 164
..$ sell
            : num 164
..$ volume : num 2
$ FGBL MAR 16:List of 6
         : num 170
..$ pl
..$ realised : logi NA
..$ unrealised: logi NA
..$ buy : num 165
..$ sell
            : num 165
..$ volume : num 2
- attr(*, "class")= chr "pl"
- attr(*, "along.timestamp")= logi FALSE
- attr(*, "instrument")= chr [1:3] "FESX JUN 16" "FGBL JUN 16" "FGBL MAR 16"
```

Each such list contains numeric vectors: 'pl', 'realised', 'unrealised', 'buy', 'sell', 'volume'. There may also be an additional vector, timestamp, to be described later in Section PL over time.

Data can be extracted by standard methods. The vectors 'realised' and 'unrealised' will be NA unless along.timestamp is not FALSE, also described in Section PL over time.

You may prefer sapply(...) instead of unlist(lapply(...)). Also, extracting the raw P/L numbers of each instrument is so common that you can say pl(pl(...)). So you could have written:

```
pl(pl(J,
    multiplier = c("FGBL" = 1000, "FESX" = 10),
    multiplier.regexp = TRUE))
```

```
FESX JUN 16 FGBL JUN 16 FGBL MAR 16
-250 10 170
```

It is often more convenient to have the data presented as a table.

```
as.data.frame(futures_pl)
```

#### 3 Computing profit and loss

```
pl buy sell volume

FESX JUN 16 -250 2910.00 2905.00 10

FGBL JUN 16 10 164.12 164.13 2

FGBL MAR 16 170 165.20 165.37 2
```

Or if you like ASCII tables, with toOrg.

```
toOrg(as.data.frame(futures_pl), row.names = "instrument")
```

We can also use pl when there are open positions. The simplest example is a journal of just one trade.

```
pl(amount = 1, price = 100)
```

There can be no P/L number since the position is not closed. But the warning message that is thrown already tells us what to do: we need to specify a price at which the open position is to be valued. This valuation price is passed as argument vprice (v as in valuation).

```
pl(amount = 1, price = 100, vprice = 105)
```

```
P/L total 5
average buy 100
average sell 105
cum. volume 1

'P/L total' is in units of instrument;
'volume' is sum of /absolute/ amounts.
```

Note that average sell takes into account the valuation price that we specified.<sup>1</sup> But cum. volume has remained 1 since only 1 unit was actually traded.

A common task is to compute P/L over a specified period of time such as one trading day. The procedure for such a case requires three ingredients:

- 1. the initial position and its valuation prices,
- 2. the trades during the period,
- 3. the final position and its prices.

Suppose yesterday, at market close, we had the following positions.

```
yesterday_position <- c("FESX JUN 16" = -20, "FGBL JUN 16" = 10)
yesterday_prices <- c("FESX JUN 16" = 2912, "FGBL JUN 16" = 164.23)
```

Note that, as with the multipliers above, we use named vectors for both the position and the prices: the names indicate the instruments.

Trading just ended, and we have done the following trades.

```
J
```

```
pl(J,
   initial.position = yesterday_position,
   initial.price = yesterday_prices,
   vprice = c("FESX JUN 16" = 2902, "FGBL JUN 16" = 164.60),
   multiplier = c("FGBL" = 1000, "FESX" = 10),
   multiplier.regexp = TRUE)
```

```
FESX JUN 16
P/L total 1750
average buy 2903.6
average sell 2910.6
```

<sup>&</sup>lt;sup>1</sup>In an earlier version of the code, average buy/sell price did not take into account vprice. But specifying vprice creates a fiction, any way (P/L 'as if' the trade was closed), and this fiction is more informative if the average buy/sell price is adjusted.

#### 3 Computing profit and loss

```
FGBL JUN 16
P/L total 3710
average buy 164.22
average sell 164.56
cum. volume 2

FGBL MAR 16
P/L total 170
average buy 165.2
average sell 165.37
cum. volume 2

'P/L total' is in units of instrument;
'volume' is sum of /absolute/ amounts.
```

We could have simulated this computation by creating one journal of the initial position and another journal (with reversed amount signs) for the final position, merging all three journals and then computing P/L.

#### 3.1.2 P/L over time

In the examples above, we computed *total* P/L. It is also illuminating to see how P/L evolved over time. Suppose that a stock trader bought one share at 50, one share at 90 and sold two shares at 100. These trades resulted in a profit of 60, or an average return of more than +40% (bought at an average price of 70, and sold at 100).

```
P/L total 60
average buy 70
average sell 100
cum. volume 4

'P/L total' is in units of instrument;
'volume' is sum of /absolute/ amounts.
```

That may appear like some pretty good trading. Yet suppose that the order of the trades was

```
buy at 90 => buy at 50 => sell at 100.
```

You may have noticed that the journal that we created above already has the trades ordered this way. We may not know what was traded and when, but there is clearly some information

in the order of the trades and the drawdown that it implies: namely a mark-to-market loss of at least 40 before it recovered. For situations like this, the argument along.timestamp can be used.

```
pl(J, along.timestamp = TRUE)
```

```
timestamp 1 2 3
P/L total 0 -40 60
__ realised 0 0 60
__ unrealised 0 -40 0
average buy 70
average sell 100
cum. volume 1 2 4

'P/L total' is in units of instrument;
'volume' is sum of /absolute/ amounts.
```

Note that we do not provide an actual timestamp, in which case the function implicitly uses integers 1, 2, ..., length(J). With no further arguments, as here, the function computes the running position and evaluates it at every trade with the trade's price. This may not be totally accurate because of bid–ask spreads or other transaction costs. But it provides more information than only computing the aggregate P/L for the trades.

```
str(pl(J, along.timestamp = TRUE))
```

In the previous section, we used vprice to value a final open position. Weu can also use it to value a position over time. See this example on quant.stackexchange.com.

## 3.2 More-complicated cases

Unfortunately, in real life computing P/L is often more complicated:

#### 3 Computing profit and loss

- One asset-price unit may not translate into one currency unit: there may be multipliers a.k.a. contract factors; there are even instruments with variable multipliers, e.g. Australian government-bond futures.
- Asset positions may map into cashflows in non-obvious ways. The simple case is the delay in actual payment and delivery of an asset, which is often two or three days. The more problematic cases are derivatives with daily adjustments of margins. In such cases, one may need to model (i.e. keep track of) the actual account balances.
- Assets may be denominated in various currencies.
- Currencies themselves may be assets in the portfolio. Depending on how they are traded (cash, forwards, &c.), computing P/L may not be straightforward.

How – or, rather, to what degree – these complications are handled is, as always, up to the user. For a single instrument, computing P/L in units of the instrument is usually meaningful, though perhaps not always intuitive. But *adding up* the profits and losses of several assets will in general not work because of multipliers or different currencies. A simple and transparent way is then to manipulate the journal before P/L is computed (e.g., multiply notionals by their multipliers).

## 4 Computing returns

## 4.1 Simple returns

The function returns computes returns from prices. The function computes what are sometimes called simple returns:  $^1$  let  $P_t$  be the price at point in time t, then

$$r_t \equiv R_t - 1 = \frac{P_t}{P_{t-1}} - 1 = \frac{P_t - P_{t-1}}{P_{t-1}}.$$
 (4.1)

For computing profit/loss in currency units, see Section Computing profit and (or) loss.

Typically, we transform a whole series  $P_{t_1}, P_{t_2}, P_{t_3}, \ldots$  into returns  $R_{t_2}, R_{t_3}, \ldots$ , which is a one-liner in R:

```
simple_returns <- function(x)
x[-1L]/x[-length(x)] - 1</pre>
```

(You may argue that these are two lines: yet even a one-liner, if used repeatedly, should be written as a function.)

Let us try it. PMWR comes with two small datasets, DAX and REXP. DAX stands for *Deutscher Aktienindex* (German Equity Index), and REXP stands for *Rentenindex* (*Performance*). Both datasets are dataframes of one column that contains the price for the day, with the timestamps stored as rownames in format YYYY-MM-DD.

```
head(DAX)
```

```
DAX
2014-01-02 9400.04
2014-01-03 9435.15
2014-01-06 9428.00
2014-01-07 9506.20
2014-01-08 9497.84
2014-01-09 9421.61
```

We extract the prices for the first five business days of 2014 and put them into a vector P.

<sup>&</sup>lt;sup>1</sup>The function never computes logarithmic returns.

```
P <- head(DAX[[1]], n = 5)
P

[1] 9400.04 9435.15 9428.00 9506.20 9497.84
```

Now we call simple\_returns.

[3,] 0.008294 0.008294 [4,] -0.000879 -0.000879

```
simple_returns(P)

[1] 0.003735 -0.000758 0.008294 -0.000879
```

In fact, using returns as provided by PMWR would have given the same result.

```
returns(P)
[1] 0.003735 -0.000758 0.008294 -0.000879
```

PMWR's returns function offers more convenience than simple\_returns. For instance, it will recognise when the input argument has several columns, such as a matrix or a dataframe. In such a case, it computes returns for each column.<sup>2</sup>

```
returns(cbind(P, P))

P P

[1,] 0.003735 0.003735

[2,] -0.000758 -0.000758
```

The argument pad determines how the initial observation is handled. The default, NULL, means that the first observation is dropped. It is often useful to use NA instead, since in this way the returns series keeps the same length as the original price series.

```
data.frame(price = P, returns = returns(P, pad = NA))
```

```
price returns
1 9400 NA
2 9435 0.003735
3 9428 -0.000758
4 9506 0.008294
5 9498 -0.000879
```

Setting pad to 0 can also be useful, because then it is easy to 'rebuild' the original series with cumprod. (But see Section Scaling series for a description of the function scale1, which is even more convenient.)

<sup>&</sup>lt;sup>2</sup>See section Vectorisation.

```
P[1] * cumprod(1 + returns(P, pad = 0))

[1] 9400 9435 9428 9506 9498
```

returns is a generic function, which goes along with some overhead. If you need to compute returns on simple data structures as in the examples above and need fast computation, then you may also use .returns. The function is the actual workhorse that performs the raw return calculation.

Besides having methods for numeric vectors (which includes those with a dim attribute, i.e. matrices) and dataframes, returns also understands zoo objects.

So let us create two zoo series, dax and rex.

```
library("zoo")
dax <- zoo(DAX[[1]], as.Date(row.names(DAX)))
rex <- zoo(REXP[[1]], as.Date(row.names(REXP)))</pre>
```

```
str(dax)
```

```
'zoo' series from 2014-01-02 to 2015-12-30
Data: num [1:505] 9400 9435 9428 9506 9498 ...
Index: Date[1:505], format: "2014-01-02" "2014-01-03" ...
```

```
str(rex)
```

```
'zoo' series from 2014-01-02 to 2015-12-30
Data: num [1:502] 441 441 442 442 ...
Index: Date[1:502], format: "2014-01-02" "2014-01-03" ...
```

```
returns(head(dax, 5), pad = NA)
```

```
2014-01-02 2014-01-03 2014-01-06 2014-01-07 2014-01-08
NA 0.003735 -0.000758 0.008294 -0.000879
```

Matrices work as well. We combine both series into a two-column matrix drax.<sup>3</sup>

```
drax <- cbind(dax, rex)
returns(head(drax, 5))</pre>
```

<sup>&</sup>lt;sup>3</sup>In case you did not know: drax is not only the name of a dataset in this book, but also the name of Marvel-comics superhero and of the villain of a James Bond novel. The latter is actually German, which makes it obvious to choose the name for representing German indices. :-)

```
dax rex
2014-01-03 0.003735 0.000611
2014-01-06 -0.000758 0.001704
2014-01-07 0.008294 0.000621
2014-01-08 -0.000879 -0.000131
```

As you see, just as for a numeric matrix, the function computes the returns for each column.

In fact, zoo objects bring another piece of information – timestamps – that returns can use. (Since xts series inherit from zoo, they will work as well.)

### 4.2 Holding-period returns

When a timestamp is available, returns can compute returns for specific calendar periods. As an example, we look at the daily DAX levels in 2014 and 2015.

```
returns(dax, period = "month")

Jan Feb Mar Apr May Jun Jul Aug Sep Oct Nov Dec YTD

2014 -1.0 4.1 -1.4 0.5 3.5 -1.1 -4.3 0.7 0.0 -1.6 7.0 -1.8 4.3

2015 9.1 6.6 5.0 -4.3 -0.4 -4.1 3.3 -9.3 -5.8 12.3 4.9 -5.6 9.6
```

If you prefer to not use zoo or xts, you may also pass the timestamp explicitly to returns.

```
returns(coredata(dax), t = index(dax), period = "month")

Jan Feb Mar Apr May Jun Jul Aug Sep Oct Nov Dec YTD

2014 -1.0 4.1 -1.4 0.5 3.5 -1.1 -4.3 0.7 0.0 -1.6 7.0 -1.8 4.3

2015 9.1 6.6 5.0 -4.3 -0.4 -4.1 3.3 -9.3 -5.8 12.3 4.9 -5.6 9.6
```

Despite the way these monthly returns are printed: the result of the function call is a numeric vector (the return numbers), with additional information added through attributes. There is also a class attribute, which has value p\_returns. The advantage of this data structure is that it is 'natural' to compute with the returns, e.g. computing means, extremes and other quantities.

```
range(returns(dax, period = "month"))
[1] -0.0928  0.1232
```

Most useful, however, is probably the print method, whose results you have seen above.

You may also compute monthly returns for matrices, i.e. for more than one asset. But now the print method will behave differently. The function's assumption is that now it would be more convenient to print the returns aligned by date in a table.

```
returns(drax, period = "month")
           dax
                rex
2014-01-31 -1.0
                1.8
2014-02-28 4.1 0.4
2014-03-31 -1.4 0.1
2014-04-30 0.5 0.3
2014-05-30 3.5 0.9
2014-06-30 -1.1 0.4
2014-07-31 -4.3 0.4
2014-08-29 0.7 1.0
2014-09-30 0.0 -0.1
2014-10-31 -1.6 0.1
2014-11-28 7.0 0.4
2014-12-30 -1.8 1.0
2015-01-30 9.1 0.3
2015-02-27 6.6 0.1
2015-03-31 5.0 0.3
2015-04-30 -4.3 -0.5
2015-05-29 -0.4 -0.2
2015-06-30 -4.1 -0.8
2015-07-31 3.3 0.7
2015-08-31 -9.3 0.0
2015-09-30 -5.8 0.4
2015-10-30 12.3 0.4
          4.9 0.3
2015-11-30
2015-12-30 -5.6 -0.6
```

If you rather wanted the other, one-row-per-year display, just call the function separately for each series.

```
lapply(list(DAX = dax, REXP = rex),
    returns, period = "month")
```

```
$DAX

Jan Feb Mar Apr May Jun Jul Aug Sep Oct Nov Dec YTD

2014 -1.0 4.1 -1.4 0.5 3.5 -1.1 -4.3 0.7 0.0 -1.6 7.0 -1.8 4.3

2015 9.1 6.6 5.0 -4.3 -0.4 -4.1 3.3 -9.3 -5.8 12.3 4.9 -5.6 9.6

$REXP

Jan Feb Mar Apr May Jun Jul Aug Sep Oct Nov Dec YTD

2014 1.8 0.4 0.1 0.3 0.9 0.4 0.4 1.0 -0.1 0.1 0.4 1.0 7.1

2015 0.3 0.1 0.3 -0.5 -0.2 -0.8 0.7 0.0 0.4 0.4 0.3 -0.6 0.5
```

See ?print.p\_returns for more display options. For instance:

```
print(returns(dax, period = "month"),
    digits = 2, year.rows = FALSE, plus = TRUE,
```

#### 4 Computing returns

```
month.names = 1:12)
    2014 2015
1 -1.00 +9.06
   +4.14 +6.61
2
   -1.40 +4.95
3
   +0.50
4
         -4.28
   +3.54
5
         -0.35
          -4.11
6
   -1.11
7
   -4.33 +3.33
8 +0.67 -9.28
9
   +0.04 -5.84
10 -1.56 +12.32
11 +7.01 +4.90
12 -1.76 -5.62
YTD +4.31 +9.56
```

Sweave There are methods toLatex and toHTML for monthly returns. In Sweave documents, you need to use results = tex and echo = false in the chunk options:

```
\begin{tabular}{rrrrrrrrrrrrr}
<<results=tex,echo=false>>=
toLatex(returns(dax, period = "month"))
\end{tabular}
```

(There is also a vignette that gives examples for toLatex; say vignette("FinTeX", package = "PMwR") to open it.)

returns accepts other values for period. For yearly returns, use period "year".

```
returns(dax, period = "year")

2014 2015
4.3 9.6

returns(drax, period = "year")

dax rex
2014 4.3 7.1
```

To get annualised returns, use period ann (or actually any string is matched by the regular expression 'ann; case is ignored).

```
returns(dax, period = "ann")

6.9% [02 Jan 2014 -- 30 Dec 2015]
```

2015 9.6 0.5

Now let us try a shorter period.

The function did *not* annualise: it refuses to do so if the time period is shorter than one year. (You may verify the return for January 2014 in the tables above.)

To force annualising, add a !. The exclamation mark serves as a mnenomic that it is now imperative to annualise.

There are several more accepted values for period, such as month-to-date (mtd), year-to-date (ytd) or inception-to-date (itd). The help page of returns lists all options. Note that any such setting for period requires that the timestamp can be coerced to Date; for instance, intraday time-series with POSIXct timestamps would work as well.

### 4.3 Returns when weights are fixed

Sometimes we may need to compute returns for a portfolio of fixed weights, given an assumption when the portfolio is rebalanced. For instance, we may want to see how a constant allocation of 10%, 50% and 40%. to three funds would have done, assuming that a portfolio is rebalanced once a month.

If more detail is necessary, then btest can be used; see Chapter Backtesting. But the simple case can be done with returns already. Here is an example.

```
[,1] [,2] [,3]
[1,] 100 2.0 3.5
[2,] 102 2.2 3.0
```

```
[3,] 104 2.4 3.1
[4,] 104 2.3 3.2
[5,] 104 2.5 3.1
```

Now suppose we want a constant weight vector, [0.1, 0.5, 0.4]', but only rebalance at times 1 and 4. (That is, we rebalance the portfolio only with the prices at timestamps 1 and 4.)

```
[1] -0.00514  0.06376  -0.01282  0.03146
attr(,"holdings")
     [,1] [,2] [,3]
[1,] 0.001 0.250 0.114
[2,] 0.001 0.250 0.114
[3,] 0.001 0.250 0.114
[4,] 0.001 0.227 0.131
[5,] 0.001 0.227 0.131
attr(,"contributions")
        [,1] [,2]
                       [,3]
[1,] 0.000000 0.0000 0.0000
[2,] 0.002000 0.0500 -0.0571
[3,] 0.002010 0.0503 0.0115
[4,] 0.000000 -0.0236 0.0108
[5,] 0.000481 0.0435 -0.0125
```

In fact, rebalancing at the first timestamp is always implied.

The result is the return series plus two additional pieces of information, stored in attributes.

**holdings** A matrix with the same dimensions as the price matrix we used as input. It provides the hypothetical holdings that were used to compute the returns. Note that these holdings only change at timestamps 1 and 4 in the example.

**contributions** Another matrix; it provides the return contributions of the single assets (in columns) in each period (in rows).

### 4.4 Return contribution

Let w(t, i) be the weight of portfolio segment i at the beginning of period t, and let r(t, i) be the return of segment i over period t. Then the portfolio return over period t,  $r_P(t)$  is a weighted

sum of the N segment returns.

$$r_{P}(t) = \sum_{i=1}^{N} r(t, i)w(t, i).$$
(4.2)

When the weights sum to unity, we may also write

$$1 + r_{P}(t) = \sum_{i=1}^{N} (1 + r(t, i)) w(t, i)$$
(4.3)

or, defining  $1 + r \equiv R$ ,

$$R_{\rm P}(t) = \sum_{i=1}^{N} R(t,i)w(t,i). \tag{4.4}$$

The total return contribution of segment i over time equals

$$\sum_{t=1}^{T-1} \left( R(t,i)w(t,i) \prod_{s=t+1}^{T} R_{P}(s) - 1 \right) + \underbrace{r(T,i)w(T,i)}_{\text{final period}}. \tag{4.5}$$

In this way, a segment's return contribution in one period is reinvested in the overall portfolio in succeeding periods.

The calculation is provided in the function rc ('return contribution').

### 4.5 Returns when there are external cashflows

The function unit\_prices helps to compute time-weighted returns of a portfolio when there are in- and outflows. (The term time-weighted returns is actually a misnomer, as returns are not weighted at all. They are only time-weighted if time-periods are of equal length.)

	timestamp	NAV	price	shares	cashflow	new_shares	total_shares	NAV_after_cf
1	2017-01-01	0	100	0.00	100	1.000	1.00	100
2	2017-01-02	101	101	1.00	0	0.000	1.00	101
3	2017-01-03	102	102	1.00	0	0.000	1.00	102
4	2017-01-04	103	103	1.00	0	0.000	1.00	103
5	2017-01-05	104	104	1.00	100	0.962	1.96	204
6	2017-01-06	205	105	1.96	0	0.000	1.96	205
7	2017-01-07	206	105	1.96	0	0.000	1.96	206
8	2017-01-08	207	106	1.96	0	0.000	1.96	207
9	2017-01-09	208	106	1.96	0	0.000	1.96	208
10	2017-01-10	209	107	1.96	0	0.000	1.96	209

The function returns a dataframe: in order to compute returns, use the price column.

# 5 Backtesting

This chapter explains how to test trading strategies with the btest function.

### 5.1 Decisions

At a given instant in time (in actual life, 'now'), a trader needs to answer the following questions:

- 1. Do I want to compute a new target portfolio, yes or no? If yes, go ahead and compute the new target portfolio.
- 2. Given the target portfolio and the actual portfolio, do I want to rebalance (i.e. close the gap between the actual portfolio and the target portfolio)? If yes, rebalance.

If such a decision is not just hypothetical, then the answer to the second question may lead to a number of orders sent to a broker. Note that many traders do not think in terms of *stock* (i.e. balances) as we did here; rather, they think in terms of *flow* (i.e. orders). Both approaches are equivalent, but the described one makes it easier to handle missed trades and synchronise accounts.

During a backtest, we will simulate the decisions of the trader. How precisely we simulate depends on the trading strategy. The btest function is meant as a helper function to simulate these decisions. The logic for the decisions described above must be coded in the functions do.signal, signal and do.rebalance.

Implementing btest required a number of decision, too: (i) what to model (i.e. how to simulate the trader), and (ii) how to code it. As an example for point (i): how precisely do we want to model the order process (e.g. use limit orders?, allow partial fills?) Example for (ii): the backbone of btest is a loop that runs through the data. Loops are slow in R when compared with compiled languages, so should we vectorise instead? Vectorisation is indeed often possible, namely if trading is not path-dependent. If we have already a list of trades, we can efficiently transform them into a profit-and-loss in R without relying on an explicit loop (see Section Computing profit and (or) loss). Yet, one advantage of looping is that the trade logic is more similar to actual trading; we may even be able to reuse some code in live trading.

Altogether, the aim for btest is to stick to the functional paradigm as much as possible. Functions receive arguments and evaluate to results; but they do not change their arguments, nor

#### 5 Backtesting

do they assign or change other variables 'outside' their environment, nor do the results depend on some variable outside the function. This creates a problem, namely how to keep track of state. If we know what variables need to be persistent, we could pass them to the function and always have them returned. But we would like to be more flexible, so we can pass an environment; examples are below. To make that clear: functional programming should not be seen as a yes-or-no decision; it is a matter of degree. And more of the functional approach can help already.

#### 5.2 Data structure

All computations of btest will be based on one or several price series of length T. Internally, these prices are stored in numeric matrices.

Prices are passed as argument prices. For a single asset, this must be a matrix of prices with four columns: open, high, low and close.

For n assets, you need to pass a list of length four: prices[[1]] must be a matrix with n columns containing the open prices for the assets; prices[[2]] is a matrix with the high prices, and so on. For instance, with two assets, you need four matrices with two columns each:

If only close prices are used, then for a single asset, use either a matrix of one column or a numeric vector. For multiple assets a list of length one must be passed, containing a matrix of close prices. For example, with 100 close prices of 5 assets, the prices should be arranged in a matrix p of size 100 times 5; and prices = list(p).

The btest function runs from b+1 to T. The variable b is the burn-in and it needs to be a positive integer. When we take decisions that are based on past data, we will lose at least one data point. In rare cases b may be zero.

Here is an important default: at time =t=, we can use information up to time t-1. Suppose that t were 4. We may use all information up to time 3, and trade at the open in period 4:

```
5 HH: MM: SS
```

We could also trade at the close:

```
open high low
     time
                                  close
1
     HH:MM:SS
2
     HH:MM:SS
                                           <-- - use information
3
                                           <-- /
     HH:MM:SS
4
                                           <-- trade here
     HH:MM:SS
                                      Χ
5
     HH:MM:SS
```

No, we cannot trade at the high or low. (Some people like the idea, as a robustness check, to always buy at the high, sell at the low. Robustness checks – forcing a bit of bad luck into the simulation – are a good idea, notably bad executions. High/low ranges can inform such checks, but using these ranges does not go far enough, and is more of a good story than a meaningful test.)

### 5.3 Function arguments

#### 5.3.1 Available information within functions

btest expects as arguments a number of functions, such as signal; see the following section for a complete list. The default is to specify no arguments to these functions, because they can all access the following 'objects'. These objects actually are, with the exception of Globals, themselves functions that can access certain data. These functions can only read; there are no replacement functions. The exception is Globals, which is an environment, and which can explicitly be used for writing (i.e. storing data).

Open open prices

High high prices

Low low prices

Close close prices

Wealth the total wealth (cash plus positions) at a given point in time

**Cash** cash (in accounting currency)

**Time** current time (an integer)

**Timestamp** the timestamp when that is specified (i.e. when the argument timestamp is supplied); if not, it defaults to Time

**Portfolio** the current portfolio

SuggestedPortfolio the currently-suggested portfolio

Globals an environment (not a function)

All functions take as their first argument a lag, which defaults to 1. So to get the most recent close price, say

```
Close()
```

which is the same as Close(lag = 1).

The lag can be a vector, too: the expression

```
Close(Time():1)
```

for instance will return all available close prices. So in period 11, say, you want close prices for lags 10, 9, ..., 1. Hence, to receive prices in their correct order, the lag sequence must always be in reverse order.

If you find it awkward to specify the lag in this reverse order, you may use the argument n instead, which specifies to retrieve the last n data points. So the above Close(Time():1) is equivalent to

```
Close(n = Time())
```

and saying

```
Close(n = 10)
```

will get you the last ten closing prices.

#### 5.3.2 Function arguments

- signal The function signal uses information until and including t-1 and returns the suggested portfolio (a vector) to be held at t. This position should be in units of the instruments; if you prefer to work with weights, then you should set convert.weights to TRUE. Then, the value returned by signal will be interpreted as weights and will be automatically converted to position sizes.
- do.signal do.signal uses information until and including t-1 and must return TRUE or FALSE to indicate whether a signal (i.e. new suggested position) should be computed. This is useful when the signal computation is costly and only be done at specific points in time. If the function is not specified, it defaults to function() TRUE. Instead of a function, this may also be

- a vector of integers, which then indicate the points in time when to compute a position, or
- a vector of logical values, which then indicate the points in time when to compute a position, or
- a vector that inherits from the class of timestamp (e.g. Date), or
- one of the keywords firstofmonth or lastofmonth (in this case, timestamp must inherit from Date or be coercible to Date).
- do.rebalance just like do.signal, but refers to the actual trading. If the function is not specified, it defaults to function() TRUE. Note that rebalancing can typically not take place at a higher frequency than implied by signal. That is because calling signal leads to a position, and when this position does not change (i.e. signal was not called), there is actually no need to rebalance. So do.rebalance is normally used when rebalancing should be done less often that signal computation, e.g. when the decision whether to trade or not is conditional on something.
- print.info The function is called at the end of an iteration. Whatever it returns will be ignored since it is called for its side effect: print information to the screen, into a file or into some other connection.
- **cashflow** The function is called at the end of each iteration; its value is added to the cash. The function provides a clean way to, for instance, add accrued interest to or subtract fees from a strategy.

### 5.4 Examples: A single asset

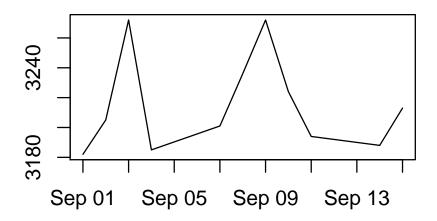
It is best to describe the btest function through a number of simple examples.

#### 5.4.1 A useless first example

I really like simple examples. Suppose we have a single instrument, and we use only close prices. The trading rule is to buy, and then to hold forever. All we need is the time series of the prices and the signal function. As an instrument we use the EURO STOXX 50 future with expiry September 2015.

### 5 Backtesting

```
timestamp prices
  2015-09-01
                3182
1
2 2015-09-02
                3205
  2015-09-03
                3272
  2015-09-04
                3185
  2015-09-07
                3201
  2015-09-08
                3236
  2015-09-09
                3272
  2015-09-10
                3224
                3194
9
  2015-09-11
10 2015-09-14
                3188
11 2015-09-15
                3213
```



The signal function is very simple indeed.

```
signal <- function()
1</pre>
```

signal must be written so that it returns the suggested position in units of the asset. In this first example, the suggested position always is 1 unit. It is only a *suggested* portfolio because we can specify rules whether or not to trade. Examples follow below.

To test this strategy, we call btest. The initial cash is zero per default, so initial wealth is also zero in this case. We can change it through the argument initial.cash.

```
(solution <- btest(prices = prices, signal = signal))
initial wealth 0 => final wealth 8
```

The function returns a list with a number of components, but they are not printed. Instead, a simple print method displays some information about the results. In this case, it tells us that the total equity of the strategy increased from 0 to 8.

We arrange more details into a data.frame. suggest is the suggested position; position is the actual position.

```
price suggest position wealth cash
1 3182 0 0 0 0
2 3205 1
3 3272 1
4 3185 1
5 3201 1
6 3236 1
                  1
                        0 -3205
                1 67 -3205
                  1 -20 -3205
1 -4 -3205
                   1
                        31 -3205
7 3272
           1
                  1
                       67 -3205
8 3224
           1
                  1
                       19 -3205
9 3194
           1
                  1 -11 -3205
                  1 -17 -3205
10 3188
           1
11 3213
                      8 -3205
```

We bought in the second period because the default setting for the burnin b is 1. Thus, we lose one observation. In this particular case here, we do not rely in any way on the past; hence, we set b to zero. With this setting, we buy at the first price and hold until the end of the data.

```
3185
                            3 -3182
5
  3201
             1
                      1
                           19 -3182
                          54 -3182
6
  3236
             1
                      1
7
                          90 -3182
   3272
             1
                      1
8
   3224
             1
                      1
                           42 -3182
9
   3194
             1
                      1
                           12 -3182
10 3188
             1
                      1
                           6 -3182
             1
                      1
11 3213
                           31 -3182
```

If you prefer the trades only, i.e. not the position series, the solution also contains a journal. (See Keeping track of transactions: journals for more on journals.)

```
journal(solution)
```

```
instrument timestamp amount price
1 asset 1 1 1 3182
1 transaction
```

To make the journal more informative, we can pass timestamp and instrument information when we call btest.

```
instrument timestamp amount price
1 FESX SEP 2015 2015-09-01 1 3182
1 transaction
```

Before we go to the next examples, a final remark, on data frequency. I have used daily data here, but any other frequency, also intraday data, is fine. btest will not care of what frequency your data are or whether your data are regularly spaced; it will only loop over the observations that it is given. It is your own responsibility to write signal (and other functions) in such a way that they encode a meaningful trade logic.

#### 5.4.2 More-useful examples

Now we make our strategy slightly more selective. The trading rule is to have a position of 1 unit of the asset whenever the last observed price is below 3200 and to have no position when it the price is above

1. The signal function could look like this.

```
signal <- function() {
   if (Close() < 3200)
        1
   else
        0
}</pre>
```

If you like to write clever code, you may as well have written this:

```
signal <- function()
Close() < 3200</pre>
```

The logical value of the comparison Close() < 3200 would be converted to either 0 or 1. But the more verbose version above is clearer.<sup>1</sup>

We call btest and check the results.

```
solution <- btest(prices = prices, signal = signal)</pre>
```

trade\_details(solution, prices)

```
price suggest position wealth cash
                       0 0
  3182 0 0
               1 0
                          0 -3205
  3205
            1
                  1 0 -3205
0 67 67
0 67 67
1 67 -3134
0 102 102
2
2 3205 1
3 3272 0
4 3185 0
5 3201 1
6 3236 0
7 3272
           0
                    0 102 102
8 3224
           0
                    0 102 102
  3194
            0
                    0
                         102 102
10 3188
            1
                     1
                          102 -3086
                  1
11 3213
                          127 -3086
```

(Yes, this strategy works better than the simple buy-and-hold, but I hope you agree that this is only because of luck.)

The argument initial.position specifies the initial position; default is no position. Suppose we had already held one unit of the asset.

Then the results would have looked as follows.

<sup>&</sup>lt;sup>1</sup>Remember what Brian Kernighan said: Everyone knows that debugging is twice as hard as writing a program in the first place. So if you're as clever as you can be when you write it, how will you ever debug it?

### trade\_details(solution, prices)

```
price suggest position wealth cash
1
  3182 1 1 3182 0
2 3205
           1
                   1 3205
                            0
          0
3 3272
                  0 3272 3272
4 3185
          0
                  0 3272 3272
                1 3272 71
0 3307 3307
0 3307 3307
0 3307 3307
5 3201
           1
6 3236 0
7 3272 0
8 3224 0
  3224
3194
            0
9
                   0
                      3307 3307
10 3188
           1
                  1 3307 119
11 3213
           1
                   1 3332 119
```

In the example above, we use the close price, but we do not access the data directly. A function Close is defined by btest and passed as an argument to signal. Note that we do not add it as a formal argument to signal since this is done automatically. In fact, doing it manually would trigger an error message:

```
signal <- function(Close = NULL) ## ERROR: argument name
1 ## 'Close' not allowed</pre>
```

```
Error in btest(prices = prices, signal = signal) :
   'Close' cannot be used as an argument name for 'signal'
```

Similarly, we have functions Open, High and Low; see Section 5.3 above for all functions.

Suppose we wanted to add a variable: a threshold that tells us when to buy. This would need to be an argument to signal; it would also need to be passed with the . . . argument of btest.

```
price suggest position wealth cash
1 3182 0 0 0 0
2 3205 1 1 0 -3205
```

```
3
   3272
                            67
                                 67
4
   3185
             0
                      0
                           67
                                 67
5
  3201
             1
                      1
                           67 -3134
6
  3236
             0
                     0
                          102
                               102
7
   3272
             0
                      0
                           102
                                102
8
             0
                      0
   3224
                           102
                                102
9
             0
                      0
   3194
                           102
                                102
              0
                      0
10 3188
                           102
                               102
                           102 -3111
11 3213
```

So far we have treated Close as a function without arguments, but actually it has an argument lag that defaults to 1. Suppose the rule were to buy if the last close is below the second-to-last close. signal could look like this.

We could also have written (Close() < Close(2L)). In any case, the rule uses the close prices of yesterday and of the day before yesterday, so we need to increase b.

```
price suggest position wealth
       0
1
 3182
                 NA
                       NA
2
  3205
           0
                 0
                       0
                 0
                      0
3
          0
 3272
4 3185
          0
                 0
                      0
5 3201
          1
                 1
                       0 -3201
         0
6 3236
                 0
                      35
                           35
7
  3272
          0
                 0
                      35
                           35
8
   3224
           0
                  0
                       35
                           35
   3194
           1
                  1
                       35 -3159
10 3188
           1
                  1
                       29 -3159
  3213
                  1
                       54 -3159
11
```

If we want to trade a different size, we have signal return the desired value.

```
price suggest position wealth cash
  3182 0 0 0 0 0
3205 2 2 0 -6410
1
2 32053 3272
            2 2 0 -6410
0 0 134 134
4 3185
             0
                      0 134 134
           2 0 0 0 0 0 2 2 3
                      2 134 -6268
5 3201
                     0 204 204
0 204 204
6 3236
  3272
7
                    0 204 204
0 204 204
0 204 204
2 204 -6172
2 254 -6172
8
  3224
  3194
9
10 3188
11 3213
```

A often-used way to specify a trading strategy is to map past prices into +1, 0 or -1 for long, flat or short. A signal is often only given at a specified point (like in 'buy one unit now'). Example: suppose the third day is a Thursday, and our rule says 'buy after Thursday'.

```
price suggest position wealth cash
1
 3182 0 0 0 0
                     0
2 3205
         0
               0
                         0
               0
                    0
3 3272
         0
                        0
              1 0 -3185
0 16 16
0 16 16
4 3185
         1
5 3201
        0
6 3236
        0
         0
               0
                   16 16
7
 3272
         0
               0
                    16
8
 3224
                        16
        0 0 16
0 0 16
0 0 16
0 0 16
9
  3194
                        16
10 3188
                        16
11 3213
                   16 16
```

But this is not what we wanted. If the rule is to buy and then keep the long position, we should have written it like this.

```
signal <- function()
if (Time() == 3L)
    1 else Portfolio()</pre>
```

The function Portfolio evaluates to last period's portfolio. Like Close, its first argument sets the time lag, which defaults to 1.

```
trade_details(btest(prices = prices, signal = signal), prices)
```

We may also prefer to specify signal so that it evaluates to a weight; for instance, after a portfolio optimisation. In such a case, you need to set convert.weights to TRUE. (Make sure to have a meaningful initial wealth: 5 percent of nothing is nothing.)

```
sp asset.1 wealth cash
   prices
    3182 0.00000 0.00000 100 100.0
2
                             100 95.0
    3205 0.00157 0.00157
3
    3272 0.00156 0.00156 100 95.0
4
   3185 0.00153 0.00153 100 95.1
   3201 0.00157 0.00157 100 95.0
   3236 0.00156 0.00157 100 95.0
6
    3272 0.00155 0.00155 100 95.0
7
   3224 0.00153 0.00153 100 95.1
3194 0.00155 0.00155 100 95.0
3188 0.00157 0.00157 100 95.0
8
9
10
11 3213 0.00157 0.00157 100 95.0
```

Note that until now we – potentially – rebalanced in every period. If you do not want that, we need to specify do.rebalance.

```
do.rebalance <- function() {
   if (sum(abs(
        SuggestedPortfolio(0) - SuggestedPortfolio())) > 2e-5)
```

```
price suggest position wealth cash

1 3182 0.0000 0.0000 100 100.00

2 3205 0.0000 0.0000 100 100.00

3 3272 0.0000 0.0000 100 100.00

4 3185 0.0306 0.0306 100 2.66

5 3201 0.0000 0.0000 100 100.49

6 3236 0.0000 0.0000 100 100.49

7 3272 0.0000 0.0000 100 100.49

8 3224 0.0000 0.0000 100 100.49

9 3194 0.0000 0.0000 100 100.49

10 3188 0.0000 0.0000 100 100.49

11 3213 0.0000 0.0000 100 100.49
```

do.rebalance is called after signal. Hence, the suggested position is known and the lag should be zero ('SuggestedPortfolio( $\theta$ )').

The tol argument works similarly: it instructs btest to only rebalance when the maximum absolute suggested change in any single position is greater than tol. Default is 0.00001, which practically means always rebalance.

```
        prices
        sp
        asset.1
        wealth
        cash

        1
        3182
        0.00000
        0.00000
        100
        100.0

        2
        3205
        0.00157
        0.00157
        100
        95.0

        3
        3272
        0.00156
        0.00157
        100
        95.0

        4
        3185
        0.00153
        0.00153
        100
        95.1

        5
        3201
        0.00157
        0.00157
        100
        95.0

        6
        3236
        0.00156
        0.00157
        100
        95.0
```

```
7 3272 0.00155 0.00155 100 95.0
8 3224 0.00153 0.00155 100 95.0
9 3194 0.00155 0.00155 100 95.0
10 3188 0.00157 0.00155 100 95.0
11 3213 0.00157 0.00157 100 95.0
```

### Passing environments

To keep information persistent, we can use environments. As an example, we store (and update) the most recent entry price.

```
notepad <- new.env()</pre>
notepad$entry <- numeric(length(prices))</pre>
signal <- function(threshold, notepad) {</pre>
    notepad$entry[Time(0L)] <- notepad$entry[Time(1L)]</pre>
    if (Close() < threshold) {</pre>
         if (Portfolio() < 1)</pre>
             notepad$entry[Time(0L)] <- Close(0L)</pre>
    } else {
         0
    }
}
solution <- btest(prices = prices,</pre>
                    signal = signal,
                    threshold = 3200,
                    notepad = notepad)
cbind(trade_details(solution, prices), entry = notepad$entry)
```

```
price suggest position wealth cash entry
1
 3182 0 0 0 0 0
2
  3205
         1
                1
                    0 -3205 3205
               0
3 3272
         0
                   67 67 3205
4 3185
               0
         0
                   67 67 3205
5 3201
         1
               1
                   67 -3134 3201
        0
               0 102 102 3201
6 3236
         0
               0
                   102 102 3201
7
 3272
               0
 3224
8
         0
                   102
                       102 3201
  3194
          0
                0
                   102
                       102 3201
10 3188
         1
               1 102 -3086 3188
               1 127 -3086 3188
11 3213
         1
```

Let us check.

```
subset(journal(solution), amount > 0)
```

btest provides an environment Globals for exactly such purposes.

```
price suggest position wealth cash entry
 3182 0 0 0
1
                              NA
2
 3205
                  1
                       0 -3205 3205
          1
                     67 67 3205
3 3272
          0
                 0
4 3185
          0
                 0
                     67
                         67 3205
                     67 -3134 3201
5 3201
          1
                 1
6
 3236
          0
                 0
                     102
                         102 3201
7
  3272
          0
                  0
                      102
                          102 3201
8
  3224
           0
                  0
                      102
                          102
                              3201
9
  3194
           0
                  0
                      102
                         102
                             3201
10 3188
           1
                  1
                     102 -3086 3188
11 3213
                     127 -3086 3188
```

### 5.5 Examples: Several assets

It does not really make a difference whether btest is called with a single or with several instruments. The pattern in signal is still to call Close() and friends to obtain data, but now these functions will return matrices with more than one column. For instance, when you have 5 assets, then Close(n = 250) would return a matrix of size 250 times 5.

### 5.5.1 A simple example

```
price.A price.B suggest.A suggest.B position.A position.B wealth cash
   100 100 0 0 NA NA NA 0
1
     98 99
98 100
97 102
96 101
98 100
                    0 0 0 0 0 0 1 0 1 0 1 0 1 2 0 0 2 0 0
                             0 0
1 0
1 0
1 0
1 0
                                                    0
                                               0
2
                                                         0
                                               1
1
                                                     0 -100
3
4
                                                     2 -100
5
                                               1
                                                     1 -100
6
                                               1
                                                     0 -100
           96
7
     97
                             1
                                      0
                                               1
                                                     -4 -100
           97
8
     98
                                      2
                                                0
                                                     -3 -199
     99
            95
                     2
9
                              0
                                       2
                                                0
                                                      -1 -199
           82
     101
                                                     3 -199
10
                                               0
```

```
journal(solution)
```

#### 5.6 Common tasks

There is more than one way to accomplish a certain task.

#### 5.6.1 Remembering an entry price

In signal, assign the current price (with lag 0) to Globals. (That is easiest because do.rebalance may not be defined.)

### 5.6.2 Delaying signals

Add a random variable to to do.rebalance:

```
if (runif(1) > prob_of_delay)
   TRUE else FALSE
```

If TRUE, rebalancing will take place.

### 5.6.3 Specifying when to compute a signal and trade

btest takes two functions, do.signal and do.rebalance, that tell the algorithm when to compute a new portfolio and when to rebalance. There are different ways to specify these dates: as a function that returns TRUE or FALSE (most general), but also as integers, logicals or actual timestamps (e.g. dates).

Supplying particular timestamps is useful when you know you want to trade on a specific calendar day, say. That is OK because you know in advance when this calendar is going to be. But be careful when you use other information to specify when to trade. The following examples are not equivalent:

```
btest(prices = prices,
    signal = signal,
    do.signal = prices > 3600)
```

```
btest(prices = prices,
    signal = signal,
    do.signal = function() Close() > 3600)
```

Loosely speaking, both variations compute a signal and trade only when prices is above 3600. But in the first version, there will be no time lag: if the prices exceeds 3600 at time  $t_i$ , we will trade at  $t_i$ . In the second example, Close() comes with a default lag of 1: if the price exceeds 3600 at  $t_i$ , we will trade at  $t_{i+1}$ , which is the more realistic case.

When timestamp is of a type that can be coerced to Date, you can also use the keywords firstofmonth and lastofmonth:

```
btest(prices = prices,
    signal = signal,
    do.signal = "firstofmonth")
```

### 5.6.4 Writing a log

Specify the function print.info. The function is called at the very end of an iteration, so it is best to use no time lag. An example

And since cat has a file argument, you can have it write such information into a logfile.

### 5.6.5 Selecting parameters: calling btest recursively

Suppose you have a strategy that depends on a parameter vector  $\theta$ . For a given  $\theta$ , the signal for the strategy would look like this.

```
signal <- function(theta) {
    ## compute position as a function of theta
}</pre>
```

Now suppose we do not know theta. We might want to test several values, and then keep the best one. For this, we need to call btest recursively: at a point in time *t*, the strategy simulates the results for various values for theta and chooses the best theta, according to some criterion f.

A useful idiom is this:

```
signal <- function(theta) {
   if (not defined theta) {
      - run btest with theta_1, ... \theta_n, select best theta
      - theta = argmin_theta f(btest(theta_i))
   }
   compute position as a function of theta
}</pre>
```

btest will first be invoked without  $\theta$  (or NULL). When the function calls signal,  $\theta$  is not defined and signal will call btest with a specified  $\theta$ .

Let us look at an actual example.

```
require("tseries")
require("zoo")
require("runStats")
## tmp <- get.hist.quote("^GSPC",</pre>
                          start = "2010-01-01",
##
##
                          end = "2013-12-31", quote = "Close")
signal <- function(Data) {</pre>
    if (is.na(Data$N)) {
        message(Timestamp(0))
        price <- Close(n = 500)
        Ns <-c(10,20)
        Data1 <- list(N = 10, hist = 200)
        res1 <- btest(price, signal, Data = Data1, b = 200)
        Data2 <- list(N = 20, hist = 200)
        res2 <- btest(price, signal, Data = Data2, b = 200)</pre>
        message("N 10 : ", round(tail(res1$wealth, 1), 2))
        message("N 20 : ", round(tail(res2$wealth, 1), 2))
        N <- if (tail(res1$wealth, 1) > tail(res2$wealth, 1))
                  10
             else
                 20
        message("N is ---> ", N, "\n")
    } else {
        N <- Data$N
    price <- Close(n = Data$hist)</pre>
    MA <- runStats("mean", price, N = N)
    pos <- 0
    if (Close() > tail(MA, 1))
        pos <- 1
    pos
}
```

# 6 Rebalancing a portfolio

### 6.1 Usage with unnamed vectors

The function rebalance computes the transactions necessary for moving from one portfolio to another. The default setting is that the current portfolio is in currency units; the target portfolio in weights. (You can change this by specifying

To compute the required order sizes, we also need the current prices of the assets. When current, target and price are unnamed, the assets' positions in the vectors need to match.

Suppose we have three stocks A, B and C with prices 1, 2 and 3. The main use case is a situation like this: you hold 50, 30 and 20 shares of these three stocks. However, suppose you have a target weight of 50%, 30% and 20%.

```
prices <- 1:3
current <- c(50, 30, 20)
target <- c(0.5, 0.3, 0.2)
rebalance(current, target, prices, match.names = FALSE)</pre>
```

Or perhaps you prefer an equal weight for every asset. Note that target now is a single number.

```
rebalance(current, target = 1/length(current),
price = prices, match.names = FALSE)
```

```
price current value % target value % order
1 1 50 50 29.4 57 57 33.5 7
2 2 30 60 35.3 28 56 32.9 -2
3 3 20 60 35.3 19 57 33.5 -1

Notional: 170. Amount invested: 170. Total (2-way) turnover: 14.
```

#### 6 Rebalancing a portfolio

However, rebalance also supports a number of special cases. Suppose you want to go into cash and close every position.

```
price current value %
                       target value %
                                         order
  1 50 50 29.4
                        0 0.0
                                          -50
2
        30 60 35.3
                               0 0.0
                                           -30
3
    3
        20 60 35.3
                           0
                               0 0.0
                                           -20
Notional: 170. Amount invested: 0. Total (2-way) turnover: 170.
```

Suppose we have no current position and want to give equal weight to each stock. Note first that we need to specify a notional. Also, rebalance now assumes that you want to invest in every stock for which a price is supplied.

```
rebalance(current = 0, target = 1/3, notional = 100,
price = prices, match.names = FALSE)
```

```
price current value %
                        target value
                                            order
                        33 33.0
   1
      0 0.0
                                              33
                                34 34.0
2
    2
          0
               0 0.0
                            17
                                              17
    3
         0
              0 0.0
                                              11
                           11 33 33.0
Notional: 100. Amount invested: 100. Total (2-way) turnover: 100.
```

### 6.2 Usage with named vectors

More usefully, rebalance can also use the names of the vectors current, target and price. The argument match.names must be set to TRUE for this (which is the default, actually).

```
prices <- c(1,1,1,1)
names(prices) <- letters[1:4]
current <- c(a = 0, b = 10)
target <- c(a = 0, d = 0.5)
rebalance(current, target, prices)</pre>
```

```
price current value % target value % order b 1 10 10 100.0 0 0 0.0 -10 d 1 0 0 0.0 5 5 50.0 5

Notional: 10. Amount invested: 5. Total (2-way) turnover: 15.
```

To also show all instruments, set the argument drop. zero to FALSE.

```
print(rebalance(current, target, prices), drop.zero = FALSE)
                          target value %
 price current value
                         0 0.0
 1 0 0 0.0
                                               0
а
b
         10
              10 100.0
                             0
                                  0 0.0
                                               -10
    1
                                  5 50.0
         0
              0 0.0
                             5
                                                5
Notional: 10. Amount invested: 5. Total (2-way) turnover: 15.
```

### 6.3 Usage with positions

In Section Keeping track of transactions: journals we used the function position to compute balances from transactions. The function may also be directly used to set up a position.

```
position(amount = 1)

position(amount = c(1,2,3), instrument = letters[1:3])
```

Note that with more than one instrument, these instruments need to be named. Otherwise, position would aggregate the positions (as it does for a journal).

```
position(amount = c(1,2,3))
```

### 6.4 Optimisation

Whenever you need to round positions, you may prefer to do an actual optimisation. The ideal place for this optimisation is the original objective function, not in rebalance. And the differences, if there are any at all, are typically small. But here is an example.

```
price lot.size
1 178 5
2 37 5
3 62 5
```

```
4
     93
5
                5
     81
6
    111
                5
7
    146
                5
8
     154
                5
9
     187
                1
                1
10 138
```

Now suppose we have only a limited budget available.

```
order
  price current value %
                      target value
                                         4
1
  178 0 0.0
                         4 712 7.1
2
    37
          0
              0 0.0
                          40 1480 14.8
                                            40
3
    62
         0
              0 0.0
                          20 1240 12.4
                                           20
4
   93
         0
              0.0
                          16 1488 14.9
                                           16
         0 0.0
0 0.0
0 0.0
5
                          13 1053 10.5
    81
                                           13
  111
                           6 666 6.7
6
                                            6
                              584 5.8
7
   146
                           4
                                            4
8
   154
         0 0.0
                          6 924 9.2
                                            6
                          5 935 9.3
9
   187
         0 0.0
                           7 966 9.7
10 138
         0
               0 0.0
Notional: 10000. Amount invested: 10048. Total (2-way) turnover: 10048.
```

Now we use TAOpt, from the NMOF package, to find the optimal integer portfolio.

```
Threshold Accepting.

Computing thresholds ... OK.
Estimated remaining running time: 0.23 secs.

Running Threshold Accepting...
Initial solution: 0.109341
Finished.
Best solution overall: 0.001108741
```

```
df <- data.frame(TA = sol$xbest, rounded = s*round(x$target/s))
df[apply(df, 1, function(i) any(i != 0)), ]</pre>
```

The difference.

[1] 0

```
ediff(sol$xbest) - ediff(s*round(x$target/s))
```

## 6.5 Substituting a basket by its components

If you run tests with baskets of instruments or whole strategies, you often need to substitute the components of the basket for overall basket. PMWR provides a function replace\_weight that helps with this task. (It is also helpful if you have hierarchies of benchmarks or want to do a 'lookthrough' through a subportfolio within your portfolio.)

Suppose we have this weight vector:

We also know what the first two baskets represent.

```
b1 <- c(a = 0.5, b = 0.2, c = 0.3)
b2 <- c(d = 0.1, e = 0.2, a = 0.7)
```

Now we can call replace\_weight.

```
basket_1::a basket_1::b basket_1::c
     0.15     0.06     0.09

basket_2::d basket_2::e basket_2::a
     0.05     0.10     0.35

basket_3
     0.20
```

If the names of the baskets or of the things in the baskets have spaces or other characters that cause trouble, quote them.

## 7 Summarising portfolio time-series

Strategies or portfolios are often analysed purely through their price (a.k.a. NAV or equity) series: more-detailed data may not be available (e.g. for a fund); or it may be more convenient to abstract from the positions to the NAV level.

To handle such series, PMWR provides an S3 class NAVseries. (I will write NAV series for the actual data series and NAVseries for the specific implementation.) An NAV series is nothing more than a time-series: a vector of NAVs, together with a vector of timestamps. Then why not simply use an existing time-series class, such as zoo? One reason is clarity. A zoo or xts object is much more general than an NAV series: it may represent more than one series; or it may represent, for instance, returns. An NAV series promises to represent NAVs (i.e. levels, not changes in levels) of a single series, nothing else. Furthermore, defining our own class allows us to define specific methods where appropriate; while the same time we may piggyback on existing time-series methods by defining methods for coercion, e.g. as.zoo.NAVseries or as.xts.NAVseries.

## 7.1 Creating NAVseries

PMWR comes with a dataset called DAX, which stands for *Deutscher Aktienindex* (German Equity Index). The dataset is a data-frame of one column that contains the price for the day, with the timestamps stored as rownames in format YYYY-MM-DD.

```
str(DAX)

'data.frame': 505 obs. of 1 variable:
$ DAX: num 9400 9435 9428 9506 9498 ...

head(DAX)

DAX

2014-01-02 9400.04
2014-01-03 9435.15
2014-01-06 9428.00
2014-01-07 9506.20
2014-01-08 9497.84
2014-01-09 9421.61
```

#### 7 Summarising portfolio time-series

We first transform the dataframe into an NAVseries by calling the function of the same name.

```
dax <- NAVseries(DAX[[1]], as.Date(row.names(DAX)), title = "DAX")
dax</pre>
```

A concise summary is printed.

```
DAX

02 Jan 2014 ==> 30 Dez 2015 (505 data points, 0 NAs)

9400.04 10743
```

There is also a generic function as. NAVseries, which can be used to coerce for instance zoo series to NAVseries.

If you have run a backtest (see Chapter Backtesting), you can extract the NAV series by saying

```
NAVseries(btest(....))
```

Note that it is NAVseries in this case, without the as prefix: That is because a call to btest returns more than just the NAV series, so the NAVseries is extracted.

## 7.2 Summarising NAV series

Most useful is probably the summary method.

```
summary(dax)
```

```
Monthly returns

Jan Feb Mar Apr May Jun Jul Aug Sep Oct Nov Dec YTD

2014 -1.0 4.1 -1.4 0.5 3.5 -1.1 -4.3 0.7 0.0 -1.6 7.0 -1.8 4.3

2015 9.1 6.6 5.0 -4.3 -0.4 -4.1 3.3 -9.3 -5.8 12.3 4.9 -5.6 9.6
```

For summaries of NAV series, a method for toLatex can be used to fill LageX-templates. The package comes with a vignette that provides examples.

## 8 Analysing trades

For some strategies or trading approaches, we may prefer to analyse trades, not equity series. (A case in point are intraday strategies, which have no exposure over night.) That is, we do not evaluate the strategy's performance at pre-defined, usually equally-spaced points in time, but rather split the trading history into separate trades.

### 8.1 Exposure

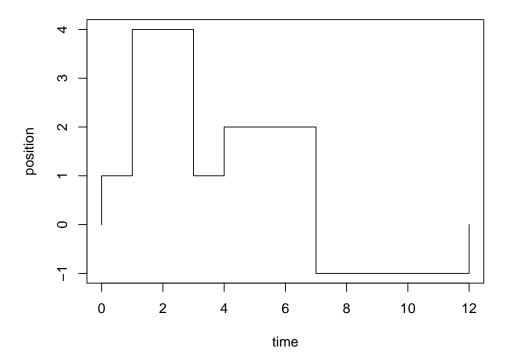
We have the following trades and times.

```
amount <- c(1,3,-3,1,-3,1)
time <- c(0,1,3,4,7,12)
```

The holding period (duration) of these trades can be computed so:

We can plot the exposure.

```
plot(c(time[1], time), cumsum(c(0, amount)),
    type = "s", xlab = "time", ylab = "position")
```



Thus, we have had a position from time 0 to time 12 (hours into the trading day, say), but its size varied. The function tw\_exposure (time-weighted exposure) computes the average *absolute* exposure.

```
tw_exposure(amount, time)
1.75
```

To give a simpler example: suppose we bought at the open of a trading day and sold at noon. The average exposure for the day is thus half a contract.

```
amount <- c(1, -1, 0)
time <- c(0,0.5,1)
tw_exposure(amount, time)
```

```
0.5
```

If we bought at the open, went short at noon, and closed the position at the end of the day, the average exposure would be one contract, since *absolute* position size is relevant.

```
amount <- c(1, -2 , 1)
time <- c(0,0.5,1)
tw_exposure(amount, time)</pre>
```

## 8.2 Splitting and rescaling

We have the following trades.

```
timestamp <- 1:3
amount <- c(-1,2,-1)
price <- c(100,99,101)
```

Calling split\_trades will return a list of two single trades. Each single trade, in turn, is a list with components amount, price and timestamp.

```
split_trades(amount, price, timestamp, aggregate = FALSE)
```

Note that the second transaction (buy 2 @ 99) has been split up: buying one contract closes the first trade; the other contract opens the second trade.

This splitting is useful in its own right: there are accounting systems around that cannot handle a trade that switches a position directly from long to short, or vice versa. Instead, the trade needs first be closed (i.e. the net position becomes zero).

#### 8 Analysing trades

With argument aggregate set to TRUE, the function reconstructs the total series, but with those trades splitted that change the position's sign.

```
split_trades(amount, price, timestamp, aggregate = TRUE)
```

```
$amount
[1] -1  1  1 -1

$price
[1] 100  99  99  101

$timestamp
[1] 1  2  2  3
```

Another example. We have the following trades and impose a limit that the maximum absolute exposure for the trader should only be 2.

```
timestamp <- 1:6
amount <- c(-1,-1,-1,1,1)
price <- c(100,99,98,98,99,100)
limit(amount, price, timestamp, lim = 2)</pre>
```

```
$amount
[1] -1 -1 1 1

$price
[1] 100 99 99 100

$timestamp
[1] 1 2 5 6
```

#### Scaling the trades.

```
scale_to_unity(amount)
[1] -0.333 -0.333 -0.333 0.333 0.333
```

Closing the trade at once.

```
close_on_first(amount)
```

```
[1] -1 -1 -1 3 0 0
```

## 9 Scaling series

Visual comparisons of time-series are ubiquitous in finance.<sup>1</sup> The function scale1 helps with scaling the levels of time-series so that is becomes easier to compare them. It is a generic function; and PMwR provides methods for numeric vectors/matrices, and for zoo and NAVseries objects.

## 9.1 Examples

To explain what the function does, we use two very short time-series: the values of the DAX, the German stock-market index, and the REXP, a German government-bond index, from 2 January and 8 January 2014 (just 5 trading days). We also combine them into a matrix drax.

```
dax <- DAX[1:5, ]
rexp <- REXP[1:5, ]
drax <- cbind(dax, rexp)</pre>
```

Calling scale1 on dax is equivalent to dividing the whole series by its first element.

```
scale1(dax) == dax/dax[1]

[1] TRUE TRUE TRUE TRUE
```

Lest you skip the rest of the chapter: scale1 comes with several additional features.

It is common, too, to scale to a level of 100. We either multiply the whole series by 100, or use the level argument.

```
scale1(dax, level = 100)

[1] 100.0000 100.3735 100.2974 101.1294 101.0404
attr(,"scale1_origin")
[1] 1
```

(The scale1\_origin attribute will be explained shortly.)

If we give a matrix to scale1, the function scales each column separately.

<sup>&</sup>lt;sup>1</sup>Transformating or scaling data are a key element of exploratory data analysis in general. See Tukey's EDA (1977). TODO: find H. Simon reference on scaling (taking reciprocal value). See also Schumann (2013).

```
scale1(drax, level = 100)
```

```
dax rexp
[1,] 100.0000 100.0000
[2,] 100.3735 100.0611
[3,] 100.2974 100.2316
[4,] 101.1294 100.2939
[5,] 101.0404 100.2807
attr(,"scale1_origin")
[1] 1
```

scale1 is a generic function; it works, for instance, with zoo objects.

```
library("zoo")
drax.zoo <- zoo(drax, as.Date(row.names(DAX)[1:5]))
scale1(drax.zoo, level = 100)</pre>
```

```
dax rexp

2014-01-02 100.0000 100.0000

2014-01-03 100.3735 100.0611

2014-01-06 100.2974 100.2316

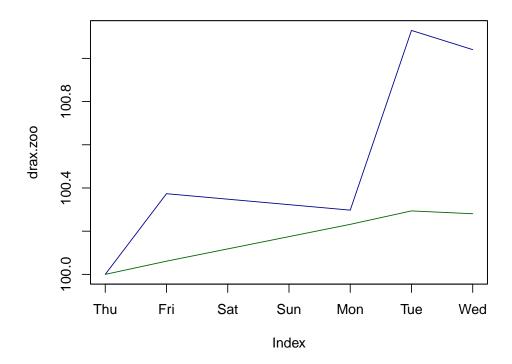
2014-01-07 101.1294 100.2939

2014-01-08 101.0404 100.2807

attr(,"scale1_origin")

[1] "2014-01-02"
```

```
plot(scale1(drax.zoo, level = 100),
    plot.type = "single",
    col = c("darkblue", "darkgreen"))
```



The argument when defines the origin.

```
scale1(drax, when = 3, level = 100)
```

```
dax rexp
[1,] 99.70344 99.76890
[2,] 100.07584 99.82987
[3,] 100.00000 100.00000
[4,] 100.82944 100.06208
[5,] 100.74077 100.04899
attr(,"scale1_origin")
[1] 3
```

This origin is attached to the scaled series as an attribute scale1\_origin. This is useful if you want mark the start of the scaled series; for instance, in a plot with abline.

With a zoo object, when should be compatible with the class of the object's index.

```
scale1(drax.zoo, when = as.Date("2014-01-07"), level = 100)
```

```
dax rexp

2014-01-02 98.88326 99.70701

2014-01-03 99.25259 99.76794

2014-01-06 99.17738 99.93796

2014-01-07 100.00000 100.00000

2014-01-08 99.91206 99.98692

attr(,"scale1_origin")

[1] "2014-01-07"
```

when also understands the keyword first.complete, which is actually the default. That is useful when some series have leading missing values.

```
drax[1:2, 1] <- NA
drax
```

```
dax rexp
[1,] NA 440.5252
[2,] NA 440.7944
[3,] 9428.00 441.5456
[4,] 9506.20 441.8197
[5,] 9497.84 441.7619
```

```
scale1(drax, level = 100) ## 'first.complete' is the default
```

```
dax rexp
[1,] NA 99.76890
[2,] NA 99.82987
[3,] 100.0000 100.00000
[4,] 100.8294 100.06208
[5,] 100.7408 100.04899
attr(,"scale1_origin")
[1] 3
```

When the argument centre is TRUE, the *mean return* is subtracted from the *returns*.

```
scale1(drax.zoo, centre = TRUE)
```

```
dax rexp

2014-01-02 1.0000000 1.000000

2014-01-03 1.0011441 0.999910

2014-01-06 0.9977916 1.000913

2014-01-07 1.0034825 1.000833

2014-01-08 1.0000000 1.000000

attr(,"scale1_origin")

[1] "2014-01-02"
```

The default is to subtract the geometric mean: the series will have a growth rate of zero; it will end where it started.

The argument scale takes a standard deviation and scales the *returns* to that standard deviation.

```
apply(returns(scale1(drax.zoo, scale = 0.02)), 2, sd)
```

```
dax rexp
0.02 0.02
```

This may create fairer comparisons, for instance, between fund prices that exhibit very different volatilities.

```
scale1(drax.zoo, scale = 0.02)
```

```
dax rexp

2014-01-02 1.000000 1.000000

2014-01-03 1.017123 1.016175

2014-01-06 1.013590 1.062012

2014-01-07 1.052132 1.079462

2014-01-08 1.047890 1.075724

attr(,"scale1_origin")

[1] "2014-01-02"
```

It should be stressed that centre and scale treat *returns*, but scale1 expects and returns *levels* (not returns).

The zoo method has a further argument that affects returns: inflate. To illustrate its use, let us create a constant series.

```
      2015-01-01
      2015-01-02
      2015-01-03
      2015-01-04
      2015-01-05
      2015-01-06

      100
      100
      100
      100
      100
      100

      2015-12-27
      2015-12-28
      2015-12-29
      2015-12-30
      2015-12-31
      2016-01-01

      100
      100
      100
      100
      100
      100
```

inflate should be a numeric value: the annual growth rate that is added to the time-series's return (or that is subtracted from it, if negative).

```
head(scale1(z, inflate = 0.02))
tail(scale1(z, inflate = 0.02))
```

```
      2015-01-01
      2015-01-02
      2015-01-03
      2015-01-04
      2015-01-05
      2015-01-06

      1.000000
      1.000054
      1.000109
      1.000163
      1.000217
      1.000271

      2015-12-27
      2015-12-28
      2015-12-29
      2015-12-30
      2015-12-31
      2016-01-01

      1.019723
      1.019779
      1.019834
      1.019889
      1.019945
      1.020000
```

## 9.2 Scaling a series: how it works

The previous section provided examples of scaling series. In this section, we are going to see how scale1 does its computations.

First, a series P passed to scale1 is transformed into returns, R. The scale argument allows you to set a desired **volatility** for the series's returns, defined as their standard deviation. The computation uses the fact that multiplying a random variable by a number b changes its variance to  $b^2$  times its original variance. Hence, scale1 divides the returns by the actual standard deviation and then multiplies them by the desired one (i.e. the value passed via the scale argument).

Changing **total return** (or average return) is slightly more complicated. Suppose we want to scale the total return of the series P such that it equals some target return  $r_*$ . Start with writing the total return as the product of single-period returns.

$$\frac{P_1}{P_0} \frac{P_2}{P_1} \cdots \frac{P_T}{P_{T-1}} = \frac{P_T}{P_0} = (1+r_1)(1+r_2)(1+r_3) \cdots = \prod_{t=1}^{T} 1 + r_t$$
 (9.1)

There clearly is an infinity of possible adjustments that would do the trick. We might, for instance, change  $P_0$  or  $P_T$  so that the desired return is achieved.

But that is probably not what we want. A reasonable requirement is that the scaling touches as few other statistical properties as possible. Adding a constant z to the return in every period does that: it does not change the volatility of the returns; neither does it affect linear or rank correlation of the returns with some other series. To compute z, we need to solve the following equation:

$$(1+r_1+z)(1+r_2+z)(1+r_3+z)\cdots = 1+r_* \tag{9.2}$$

Alternatively, we may use logs.

$$\sum_{i} \log(1 + r_i + z) = \log(1 + r_*) \tag{9.3}$$

This is an application for root-finding (see chapter 11 of (Gilli, Maringer, and Schumann, 2011)), for which scale1 uses uniroot.

As 'computational proof', we create two series P1 and P2.

```
P1 <- cumprod(1 + c(0, rnorm(20, sd = 0.02)))
P1_scaled <- scale1(P1, centre = TRUE)

P2 <- cumprod(1 + c(0, rnorm(20, sd = 0.02)))
P2_scaled <- scale1(P2, centre = TRUE, scale = 0.03)
```

Centring does not change the standard deviation.

```
sd(returns(P1))
sd(returns(P1_scaled))
```

```
[1] 0.01893257
[1] 0.01893257
```

But centring affects the total return, which becomes zero.

```
tail(P1,1)
tail(P1_scaled,1)
```

```
[1] 0.8315632
[1] 1
```

Using scale affects the standard deviation.

```
sd(returns(P2))
sd(returns(P2_scaled))
```

```
[1] 0.02178837
[1] 0.03
```

Scaling the series does not affect correlation.

```
cor(returns(P1), returns(P2))
cor(returns(P1_scaled), returns(P2_scaled))
```

```
[1] -0.3675171
[1] -0.3675171
```

# 10 Plotting irregularly-spaced series during trading hours

## 10.1 An example

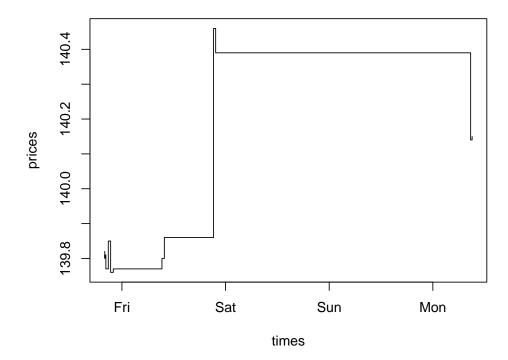
We have the following sample of prices of the Bund future contract, traded at the Eurex in Germany.

times	prices
2012-10-18 20:00:09	139.82
2012-10-18 20:01:11	139.82
2012-10-18 20:01:59	139.8
2012-10-18 20:01:29	139.81
2012-10-18 20:16:49	139.77
2012-10-18 20:50:49	139.85
2012-10-18 21:23:19	139.76
2012-10-18 21:41:39	139.76
2012-10-18 21:59:59	139.77
2012-10-19 09:16:10	139.8
2012-10-19 09:49:31	139.86
2012-10-19 21:12:49	140.46
2012-10-19 21:42:31	140.39
2012-10-22 08:45:15	140.14
2012-10-22 09:05:33	140.15

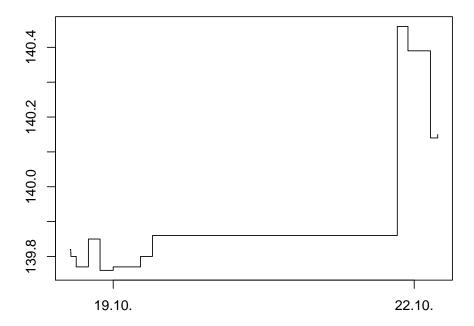
Note that I have left the time zone to the operating system. Since my computer is typically located in the time zone that the tz database (http://www.iana.org/time-zones) calls 'Europe/Berlin', the first time should be 2012-10-18 20:00:09. If, for instance, your computer is in 'America/Chicago' instead and you run the above code, the first time would be 2012-10-18 13:00:09. Which is right: it is the correct time, only translated into Chicago local time.

A plot of price against time looks like this.

```
plot(times, prices, type = "s")
```



Such a plot is fine for many purposes. But the contract for which we have prices is only traded from Monday to Friday, not on weekends, and it is traded only from 08:00 to 22:00 Europe/Berlin time. So the plot should omit those times at which no trading takes place. This is what the function plot\_trading\_hours does.



What we need for such a plot is a function that maps actual time to a point on the x-scale, while the y-scale stays unchanged. If we were talking only about days, not times, we needed something like this:

day	<i>x</i> -position	mapped <i>x</i> -position
Thursday	1	1
Friday	2	2
Saturday	3	<removed></removed>
Sunday	4	<removed></removed>
Monday	5	3

This mapping is what plot\_trading\_hours provides. And not much more: the design goal of the function is to make it as much as possible an ordinary plot; or more specifically, to make it as similar as possible to the plot function. Indeed, plot\_trading\_hours calls plot with a small number of default settings:

```
list(type = "l", xaxt = "n", xlab = "", ylab = "")
```

These settings can all be overridden through the ... argument, which is passed to plot. Note that we already set s as the plot's type in the last code chunk. The only required setting is suppressing the x-axis with setting xaxt to 'n', because plot\_trading\_hours will create its own x-axis via a call to axis(1, ...). In case you wish to use your own axis specification, either set do.plotAxis to FALSE or pass settings to axis through the list axis1.par.

## **10.2** More examples

#### 10.2.1 Value of plot\_trading\_hours

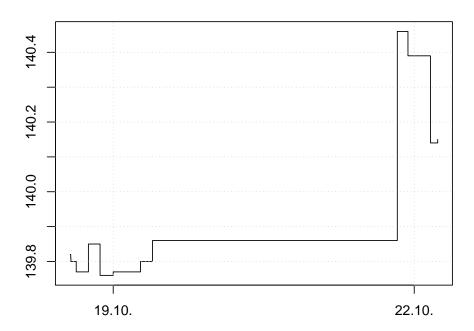
Like plot, plot\_trading\_hours is typically called for its side effect: creating a plot. But it also returns useful information (invisibly, unless called with do.plot = FALSE).

```
str(tmp)
```

This information can be used to add elements to plots. An example follows.

#### 10.2.2 Adding grid lines

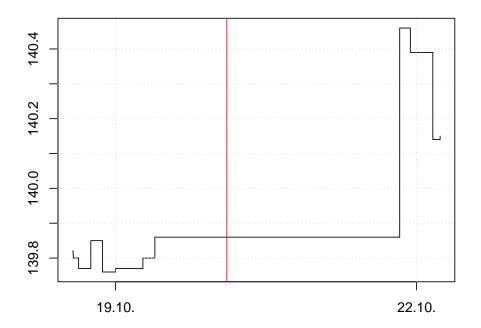
We can add grid lines with abline. The y-axis poses no special problem. The positions of the x-axis ticks are returned from plot\_trading\_hours.



If we wan to add to a specific time, say 19 October, 13:10:23, we can use the function map that the call to plot\_trading\_hours returns. We first create the specific time with, for example, ISOdatetime or strptime.

```
[1] "2012-10-19 13:10:23 CEST"
```

Now we use map to translate this time into the appropriate x-position.



The function map returns a list with two components, t and ix.

```
tmp$map(mytime)

$t
[1] 25816

$ix
[1] 1
```

The first component is the appropriate position on the x-axis; since it is a time it is called t. The second component gives the subscripts to values that should actually be plotted. As an example, suppose that we wish to plot points at several prices at 21:00:00 for several days.

```
times weekday values
1 2012-10-18 21:00:00 Thursday 140.0
2 2012-10-19 21:00:00 Friday 140.1
3 2012-10-20 21:00:00 Saturday 140.2
```

But 20 October 2012 is a Saturday, and so it does not appear in the plot.

```
tmp$map(moretimes)
```

```
$t
[1] 3592 53993

$ix
[1] 1 2
```

The values that should be plotted can conveniently be found by using ix.

```
values[tmp$map(moretimes)$ix]
```

```
[1] 140.0 140.1
```

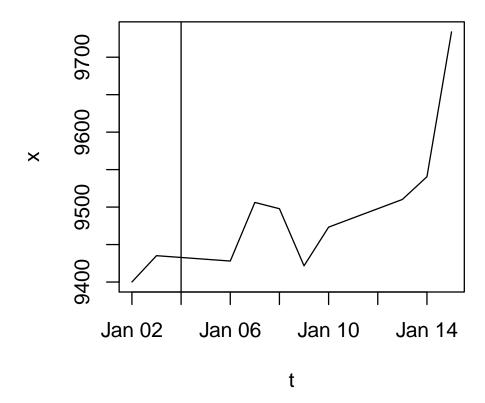
## 10.3 Daily data

plot\_trading\_hours also handles data on a daily frequency. The function will assume such a case if the timestamp is of class Date; it will then choose sensible defaults for the time-axis. In effect, the function will remove weekends and, if specified, holidays.

As an example, consider the first 10 observations of the DAX dataset.

```
x <- DAX[1:10, ]
t <- as.Date(row.names(DAX)[1:10])
data.frame(t, x, weekday = weekdays(t))</pre>
```

If we plot these data, there will be a value plotted for 2014-01-04, as marked by the vertical line.

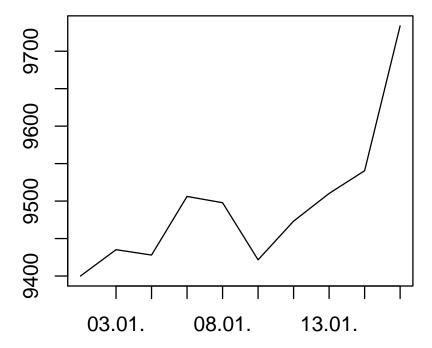


That is despite the fact that this is a Saturday.

```
format(as.Date("2014-01-04"), "%A")
```

```
Saturday
```

This is not a bug: it is the default behaviour of plot. Saturday's value results from an interpolation. plot\_trading\_hours instead ignores such nonexisting dates.



## 11 Other Tools

## 11.1 Dividend adjustments

The function div\_adjust corrects price series for dividends. It is meant as a low-level function and is implemented to work on numeric vectors. Consider a hypothetical price series x, which goes ex-dividend at time 3.

```
x <- c(9.777, 10.04, 9.207, 9.406)
div <- 0.7
t <- 3
```

The default for div\_adjust is to match the final price.

```
div_adjust(x, t, div)
[1] 9.086185 9.330603 9.207000 9.406000
```

If you prefer a correction that matches the first price, set argument backward to FALSE.

```
div_adjust(x, t, div, backward = FALSE)
[1] 9.77700 10.04000 9.90700 10.12113
```

## 11.2 Stocks splits

The function split\_adjust handles stock splits. It is implemented to work on numeric vectors.

## 11.3 Treasuries quotes

US treasury bonds are often quoted in 1/32nds of points. For instance, the price 110'030 would mean 110+3/32. The function quote 32 provides a way to 'pretty-print' such prices.

```
quote32(c("110-235", "110-237"))
```

```
110-23+
110-23<sup>1</sup>/<sub>4</sub>
```

Internally, quote32 will store the prices as numeric values: the fractions are only used for printing.

```
as.numeric(quote32(c("110-235", "110-237")))
[1] 110.7344 110.7422
```

## 11.4 Validating ISINs

An ISIN, which stands for International Securities Identification Number, uniquely<sup>1</sup> identifies a security.

#### 11.5 Price tables

A pricetable is a matrix of prices, with some added functionality for subsetting.

#### 11.6 Trees

To *normal people*, a tree consists of a trunc, branches and leaves. To *people who do graph theory*, a tree is a connected graph with only one path between any two nodes.

Trees are useful to represent hierachies – just think of a file tree.

<sup>&</sup>lt;sup>1</sup>More or less uniquely, depending on the definition of security. ISINs are widely used for equities, in particular in European markets. But note that ISINs do not contain information about the trading venue. Also, for derivatives, an ISIN may not uniquely identify the contract: for instance, Euro-Bund Futures, traded at the Eurex, have a single ISIN for all maturities.

## 12 FAQ/FRC

## (Frequently-required computations)

I have a list of timestamped trades and I need to compute P/L between two points in time, for instance between yesterday's evening close and now (intraday).

Call the points in time  $t_0$  and  $t_1$ . The easiest case is if there were no positions at both  $t_0$  and  $t_1$ . In that case, create a journal of your trades, and call pl.

If there were positions, you will need the valuation prices for all instruments with positions at both points in time. Then, you can use pl; see arguments initial.position and vprice.

Alternatively, you would arrive at the P/L as follows:

- 1. Compute the position at  $t_0$  and make it a journal  $J_0$ . The prices need to be the valuation prices. (That is, pretent you opened the position at their valuation prices at  $t_0$ .)
- 2. Take all transactions at  $t > t_0$  and  $t \le t_1$  and put them into a journal J.
- 3. Compute the position at  $t_1$  make it a journal  $J_1$ , and multiply all amounts by -1. The prices need to be the valuation prices. (That is, pretent you closed the position at their valuation prices at  $t_1$ .)
- 4. Combine  $J_0$ , J, and  $J_1$  and compute the P/L.

How can I compute portfolio returns when I don't have prices, but only returns of the assets?

Compute artificial prices; e.g. using something like

cumprod(c(1, 1 + r))

Then use returns.

I have a portfolio with constant weights. How to compute its returns when it is rebalanced at specific times?

Compute artificial prices, and then use returns: see arguments weights and rebalance. when. See Section Returns when weights are fixed.

I have a list of trades: instrument, side (buy/sell), quantity, when and at what price. How to compute the profit and loss for each?

See pl.

I have a list of trades in an instrument and want to plot these trades against the price of the traded instrument.

Use pl; in particular, pass the prices with vprice.

I have a signal series (+1, 0, 0, +1, ...), and need to transform it into a profit-and-loss series.

If these are positions, pass the signals to btest and access them with signals[Time()].

I need to determine the month-to-date profit-and-loss.

- 1. compute position on last day of last month
- 2. make journal from position (add prices)
- 3. combine with journal since month start
- 4. use ~pl on all instruments

btest: I want to print my current P/L in every period.

Use print.info.

btest: I invest in assets that pay accrued interest.

Directly work with the dirty prices. If the signals depend on clean prices, pass them as extra information and access them with clean\_price[Time()]. Alternatively, work with the clean prices, and use cashflow to add the accrued interest to the cash account.

btest: Can I rebalance more frequently than I compute a signal?

You can, but it does not make sense in the standard setup. That is, no rebalancing will take place, even if you instruct btest to do so. The reason is that a signal computes a suggested position (in units of the instrument); once this position has been built up, no more trading is required. This is even true when using weights: The argument convert.weights is a convenience that converts weights into a suggested position; btest does not store these weights, only the suggested position.

## 13 Appendix: Classes and data structures

The following classes are implicitly defined (i.e. they are S3 classes):

journal keeps transactions. Internally, a object of class journal is named list of atomic vectors.

**position** the numerical positions of different accounts/instruments at specific points in time. Always stored in a numeric matrix with attributes timestamp and instrument; points in time are in rows, instruments in columns.

**period returns** numeric vector (potentially a matrix) with attributes timestamp and period. The class is called p\_returns

instrument term sheet (description etc); it does know nothing about market data - not yet implemented

cashflow internal - not yet implemented

**NAVseries** store a time-series of net asset values

**pricetable** a matrix of NAVs (or prices); each column corresponds to one asset. Additional attributes instrument and timestamp. Often, pricetables will be created corresponding to positions.

# 14 Appendix: Notes for developers

## 14.1 Methods for returns

Methods are responsible for 'stripping' the input down do x and t, calling 'returns.default' or some other method, and then to re-assemble the original class's structure. When period is not specified, methods should keep timestamp information for themselves and not pass it on. That is, returns.default should only ever receive a timestamp when period is specified.

## 15 Appendix: R and package versions used

```
R version 3.4.2 (2017-09-28)
Platform: x86_64-pc-linux-gnu (64-bit)
Running under: Ubuntu 17.04
Matrix products: default
BLAS: /usr/lib/openblas-base/libblas.so.3
LAPACK: /usr/lib/libopenblasp-r0.2.19.so
locale:
[9] LC_ADDRESS=C
                            LC_TELEPHONE=C
[11] LC_MEASUREMENT=en_IE.UTF-8 LC_IDENTIFICATION=C
attached base packages:
[1] stats graphics grDevices utils datasets methods
[7] base
other attached packages:
[1] rbenchmark_1.0.0 zoo_1.7-14 orgutils_0.4-2
[4] PMwR_0.5-8
loaded via a namespace (and not attached):
[1] datetimeutils_0.2-7 compiler_3.4.2
[4] fastmatch_1.0-4 crayon_1.3.4
                                        parallel_3.4.2
                                        NMOF_1.2-0
                     textutils_0.1-8 lattice_0.20-35
[7] grid_3.4.2
```

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